

6.6 Solute Transport During Variably Saturated Flow— Inverse Methods

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6.6.1 Introduction

The use of parameter estimation techniques for determining soil hydraulic properties is well established (Kool et al., 1987; Hopmans & Šimůnek, 1999; Sections 1.7 and 3.6.2). The approach has been widely used for various laboratory and field experiments. Among others, laboratory experiments include one-step and multistep outflow experiments, upward flux or head-controlled infiltration, the evaporation method, and others (Section 3.6.2). In separate lines of research, solute transport parameters are often obtained from column experiments assuming steady-state water flow (e.g., Nkedi-Kizza et al., 1984; Sections 6.3–6.5), and using parameter estimation codes such as CFITIM (van Genuchten, 1981), CXTFIT (Toride et al., 1995), or STANMOD (Šimůnek et al., 1999) for fitting analytical solutions of the transport equation to experimental breakthrough curves. Obtaining solute transport parameters for conditions for which no analytical solutions exist, such as for nonlinear adsorption, can be accomplished using numerical solutions (Kool et al., 1989; Šimůnek & van Genuchten, 1999).

The above parameter estimation efforts for water flow and solute transport have thus far remained relatively disjointed. Although numerous studies exist that combine estimation of flow and transport parameters for groundwater flow problems (e.g., Sun & Yeh, 1990; Medina & Carrera, 1996; Weiss & Smith, 1998), only a few studies have used combined transient variably saturated water flow and solute transport experiments for simultaneous estimation of soil hydraulic and solute transport parameters (Mishra & Parker, 1989; Abbaspour et al., 1997; Inoue et al., 2000; Jacques et al., 2001).

Different strategies in combined estimation of water flow and solute transport parameters can be followed (Inoue et al., 2000). First, one could use water flow information only (e.g., pressure heads and/or fluxes) to estimate the soil hydraulic parameters, followed by estimation of the transport parameters using information

from the transport part of the experiment (e.g., solute concentrations). Alternatively, combined water flow and transport information can be used to estimate soil hydraulic and solute transport parameters in a sequential manner. Finally, combined water flow and transport information can be used to simultaneously estimate both the soil hydraulic and solute transport parameters. This last approach is the most beneficial since it uses crossover effects between state variables and parameters (Sun & Yeh, 1990), and it takes advantage of all available information since concentrations are a function of water flow (Medina & Carrera, 1996). Mishra and Parker (1989) showed that simultaneous estimation of hydraulic and transport properties yields smaller estimation errors for model parameters than sequential inversion of hydraulic properties from water content and matric pressure head data, followed by inversion of transport properties from concentration data.

In this section we focus on the application of parameter estimation methods to indirect estimation of the soil hydraulic and solute transport parameters from variably saturated transient flow experiments. Since the approach requires the use of numerical methods, we also include a relatively simple example involving transport of solute with nonlinear chemical reaction (during steady water flow) for which no analytical solution is available. Parameter estimation methods coupled with comprehensive numerical models can provide extremely useful tools for analyzing experimental data that may not be evaluated optimally using conventional tools such as analytical solutions (Sections 6.3 through 6.5). Because of the generality of numerical models, these tools are very attractive for analyzing conveniently and accurately a broad range of steady-state and transient laboratory and field flow and transport experiments.

General reviews of the application of inverse modeling was presented by Hopmans and Šimůnek (1999) and in Section 1.7. Specific applications to variably saturated flow problems only are discussed in Section 3.6.2. We will briefly present the governing equations for simultaneous variably saturated water flow and nonlinear nonequilibrium solute transport, define the inverse problem, and then give four examples demonstrating the application of parameter estimation techniques to solute transport problems of increasing complexity. The first example deals with nonlinear solute transport in a laboratory column. The second example applies the parameter estimation method to a laboratory column experiment that used a flow interruption technique to evaluate rate-limited mass transfer. The third example deals with variably saturated water flow and solute transport during an infiltration experiment in a laboratory column. Finally, the fourth example describes a relatively complex field experiment involving time-dependent boundary conditions, a layered soil profile, and nonequilibrium solute transport. We will devote little attention to questions of uniqueness, stability, parameter confidence intervals, and strengths and weaknesses of the approach, since these topics are extensively discussed in Sections 1.7 and 3.6.2.

6.6.2 Theory of Flow, Transport, and Optimization

Isothermal one-dimensional Darcian water flow in a variably saturated rigid isotropic porous medium is given by the following modified form of the Richards equation:

$$\frac{\partial \theta}{\partial t} = - \frac{\partial q}{\partial z} - S = \frac{\partial}{\partial z} \left[K \left(\frac{\partial h}{\partial z} + 1 \right) \right] - S \quad [6.6-1]$$

where θ is the volumetric water content, h is the pressure head, q is the volumetric flux density, z is the vertical coordinate positive upwards, t is time, S is a sink term, and K is the unsaturated hydraulic conductivity function. Various analytical expressions can be used to describe the retention and hydraulic conductivity functions (Section 3.3.4).

Solute transport during transient water flow in a variably saturated rigid porous medium is given by:

$$\frac{\partial \theta c}{\partial t} + \frac{\partial \rho s}{\partial t} = \frac{\partial}{\partial z} \left(\theta D \frac{\partial c}{\partial z} \right) - \frac{\partial qc}{\partial z} - Sc_r - \mu_w \theta c - \mu_s \rho s + \gamma_w \theta + \gamma_s \rho \quad [6.6-2]$$

where c and s are solute concentrations in the liquid and solid phases, respectively; ρ is the soil bulk density, μ_w and μ_s are first-order rate constants for solutes in the liquid and solid phases, respectively; γ_w and γ_s are zero-order rate constants for the liquid and solid phases, respectively; S is the sink term in the flow equation (Eq. [6.6-1]), c_r is the concentration of the sink term, and D is the dispersion coefficient for the liquid phase:

$$D = D_w \tau + \lambda |v| \quad [6.6-3]$$

where D_w is the molecular diffusion coefficient, τ is a tortuosity factor, λ is the longitudinal dispersivity, and v is the average pore water velocity ($= q/\theta$).

Interactions between the solution (c) and adsorbed (s) concentrations can be described in terms of equilibrium and nonequilibrium models. For equilibrium adsorption, the isotherm relating s and c may be described by a generalized nonlinear equation of the form

$$s = k_d c^\beta / (1 + \eta c^\beta) \quad [6.6-4]$$

where k_d , β , and η are empirical coefficients. The Freundlich, Langmuir, and linear isotherms are special cases of Eq. [6.6-4].

Nonequilibrium sorption is usually described by a mass transfer reaction where the transfer between solutes in the solution and the sorbed phases is governed by the concentration differences and a mass transfer coefficient α_{mt} :

$$\partial s / \partial t = \alpha_{mt} [k_d c^\beta / (1 + \eta c^\beta) - S] \quad [6.6-5]$$

It has often been observed that sorption sites can be separated into two types. Type-1 sorption sites (fraction f) undergo instantaneous sorption, described by Eq. [6.6-4], whereas the remaining type-2 sorption sites (fraction $1 - f$) undergo nonequilibrium sorption, described by Eq. [6.6-5]. This concept is known as the two-site sorption model (e.g., Selim et al., 1977; van Genuchten & Wagenet, 1989). The general mass balance equation for the type-2 sorption sites is then given by

$$\frac{\partial s_k}{\partial t} = \alpha_{mt} \left[(1-f) \frac{k_d c^\beta}{1 + \eta c^\beta} - s_k \right] \quad [6.6-6]$$

where s_k is the sorbed phase concentration at the kinetically controlled sorption sites.

Physical nonequilibrium transport may also exist (Section 6.3). Physical nonequilibrium may be implemented using the concept of two-region dual-porosity type transport (van Genuchten & Wierenga, 1976) by assuming that the liquid phase can be partitioned into mobile (flowing), θ_m , and immobile (stagnant), θ_{im} , regions, and that solute exchange between the two liquid regions can be modeled as a first-order process; that is,

$$\frac{\partial \theta_m c_m}{\partial t} + \frac{\partial f' \rho s_m}{\partial t} = \frac{\partial}{\partial z} \left(\theta_m D_m \frac{\partial c_m}{\partial z} \right) - \frac{\partial q_m c_m}{\partial z} - S c_r - \alpha'_{mt} (c_m - c_{im}) \quad [6.6-7]$$

$$\left[\theta_{im} + \rho(1-f') \frac{k_d \beta c_{im}^{\beta-1}}{(1 + \eta c_{im}^\beta)^2} \right] \frac{\partial c_{im}}{\partial t} = \alpha'_{mt} (c_m - c_{im}) \quad [6.6-8]$$

where c_{im} is the concentration of the immobile region, α'_{mt} the mass transfer coefficient for exchange between the two liquid regions, f' is the fraction of exchange sites in contact with the immobile solution phase, and the subscript “m” refers to the mobile region. Notice that the parameters f' and α'_{mt} in Eq. [6.6-8] have a slightly different meaning than f and α_{mt} in Eq. [6.6-6].

Equations [6.6-1] through [6.6-8] must be solved numerically for variably saturated flow and/or nonlinear solute transport problems for a given set of initial and boundary equations. When the van Genuchten (1980) analytical expression for the soil hydraulic properties is used, the optimized soil hydraulic parameters may include the residual, θ_r , and saturated, θ_s , water contents, the saturated hydraulic conductivity, K_s , and the shape parameters n , α , and l (Section 3.3.4). The optimized solute transport parameters for solute transport as described with Eq. [6.6-2] through [6.6-8] could include the following parameters: D_w , f , f' , k_d , β , θ_{im} , η , α_{mt} , α'_{mt} , τ , and/or λ .

The objective function, Φ , to be minimized during the parameter estimation process may be defined as

$$\Phi(\mathbf{b}, \mathbf{y}) = \sum_{j=1}^m v_j \sum_{i=1}^{n_j} w_{ij} [y_j^*(z, t_i) - y_j(z, t_i, \mathbf{b})]^2 \quad [6.6-9]$$

where the right-hand side represents the residuals between the measured (y_j^*) and corresponding model predicted (y_j) space-time variables, using the vector of optimized soil hydraulic and solute transport parameters, \mathbf{b} . The first summation sign sums residuals for different measurement types, m , whereas the variable n_j in the second summation denotes the number of measurements for a certain measurement type. The factors w and v are weighting factors for the individual measurements and the measurement types, respectively. For instance, w can represent the standard deviation or analytical errors for measurements. We assume weighting factors w to be equal to unity, and factors v are defined as follows:

$$v_j = 1/(n_j \sigma_j^2) \quad [6.6-10]$$

where σ_f^2 is the variance of the measurements y_f^* . Measured values can include water flow variables—such as water contents, pressure heads, and/or water fluxes; solute transport variables—such as concentrations and/or solute fluxes; or integral variables—such as electrical conductivity. Minimization of the objective function (Eq. [6.6–9]) can be carried out using optimization techniques discussed in Section 1.7.

6.6.3 Examples

We demonstrate the use of the parameter estimation method with four examples of increasing complexity, using the variably saturated water flow and solute transport numerical model HYDRUS-1D (Šimůnek et al., 1999) for each example. However, any suitable numerical flow and transport code could be used for this purpose.

The first example deals with transport of solute with nonlinear chemical reaction in a fully saturated laboratory column. Parameters of the nonlinear Freundlich adsorption isotherm are obtained by analyzing a measured breakthrough curve. In the second example, we applied parameter estimation to a laboratory column experiment that used the flow interruption technique to evaluate rate-limited mass transfer. The third example involves variably saturated water flow and equilibrium solute transport during infiltration in a laboratory column. The soil hydraulic and solute transport parameters are optimized simultaneously in this example. The fourth and final example uses data from a relatively complex field experiment involving atmospheric boundary conditions, a layered soil profile, and nonequilibrium solute transport. The soils hydraulic and solute transport parameters for individual soil layers are obtained sequentially. This example considers nonequilibrium solute transport using the mobile–immobile dual porosity concept.

6.6.3.1 Steady-State Laboratory Flow Experiment with Nonlinear Transport

The first example demonstrates the use of the inverse procedure for the estimation of nonlinear sorption parameters from a column breakthrough curve reported by Selim et al. (1987). A 10.75-cm-long soil column was first saturated with a 0.005 *M* CaCl₂ solution. The transport experiment consisted of applying a 14.26 pore volume pulse ($t = 358.05$ h) of a 0.005 *M* MgCl₂ solution, followed by the original CaCl₂ solution. The flow rate was equal to 6.495 cm d⁻¹. The adsorption isotherm was determined independently with the help of batch experiments (Selim et al., 1987), and fitted with the Freundlich equation, to yield $k_d = 1.69$ cm³ g⁻¹ and $\beta = 1.62$.

Only the dispersion coefficient (D) and the Freundlich coefficients (Eq. [6.6–4] with $\eta = 0$) k_d and β were optimized in this example. Since the governing solute transport equation is nonlinear, no analytical solution is available, so that one must resort to a numerical model. The soil profile was discretized using 44 nodes, and a third-type boundary condition was used at the top of the column. The observed and fitted Mg breakthrough curves are shown in Fig. 6.6–1. The results indicate a reasonable prediction of the measured breakthrough curve for the final estimates of the optimized solute transport parameters ($\lambda = 3.76 \pm 1.40$ cm, $k_d = 1.44 \pm 1.14$ cm³ g⁻¹, and $\beta = 1.62 \pm 0.35$). A very high negative correlation of $r^2 = -0.99$ was found between the sorption parameters k_d and β .

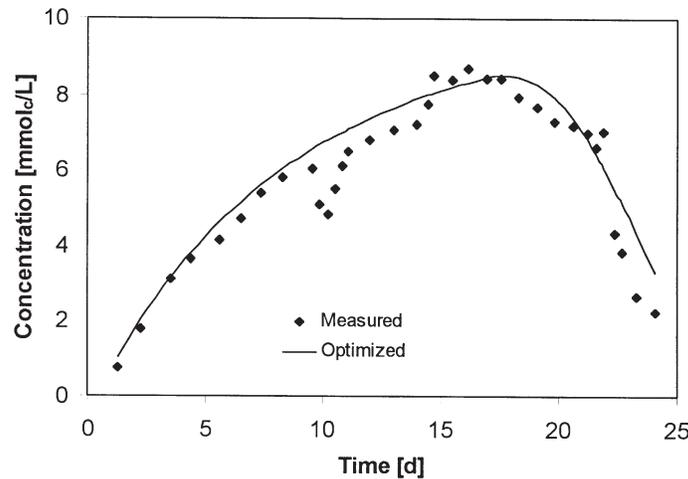


Fig. 6.6-1. Measured and fitted Mg breakthrough curves for Abist loam (data taken from Selim et al., 1987).

6.6.3.2 Laboratory Transport Subject to Flow Interruption

In the second example, we analyzed a column breakthrough curve (Fortin et al., 1997) obtained using the flow interruption technique. Flow interruption techniques are often used to elucidate rate-limited sorption processes (Murali & Aylmore, 1980; Brusseau & Rao, 1989; Fortin et al., 1997). This particular experiment was carried out in a 15-cm-long repacked soil column (loamy sand). The bulk density was 1.41 g cm^{-3} and the saturated water content $0.47 \text{ cm}^3 \text{ cm}^{-3}$. The experiment was performed under steady-state, fully saturated flow conditions in a vertical direction at a flow rate of 0.674 cm h^{-1} , corresponding to a pore water velocity v of 1.43 cm h^{-1} . Bromide and the herbicide simazine (6-chloro-*N,N'*-diethyl-1,3,5-triazine-2,4-diamine) were dissolved in a 0.01 M CaSO_4 solution at concentrations of 50 mg L^{-1} and $0.025 \text{ } \mu\text{g L}^{-1}$, respectively, and introduced into the column as step inputs. Flow was stopped for 185 h after five pore volumes of input. Fortin et al. (1997) analyzed the bromide and simazine breakthrough curves using equilibrium and nonequilibrium solute transport models, respectively. They used three nonequilibrium models (i.e., a two-stage, two-rate; a two-stage, one-rate; and rate-limited sorption models) and concluded that the two-stage, two-rate model, in which the first rate proceeds considerably faster than the second one, could describe simazine breakthrough data the best.

Here we illustrate the parameter optimization procedure using the two-site sorption model (Eq. [6.6-2] and [6.6-6]). First, the bromide breakthrough curves were used to estimate the hydrodynamic dispersion of the column system. Flow interruption experiments indicated that bromide was not subject to chemical or physical nonequilibrium processes. The fitting of the steady-state solute transport equation to the bromide breakthrough data yielded a dispersivity of $\lambda = 0.341 \pm 0.011 \text{ cm}$ (bromide breakthrough curve not shown). This dispersivity was then used as a fixed parameter in the subsequent estimation of the sorption parameters. It is as-

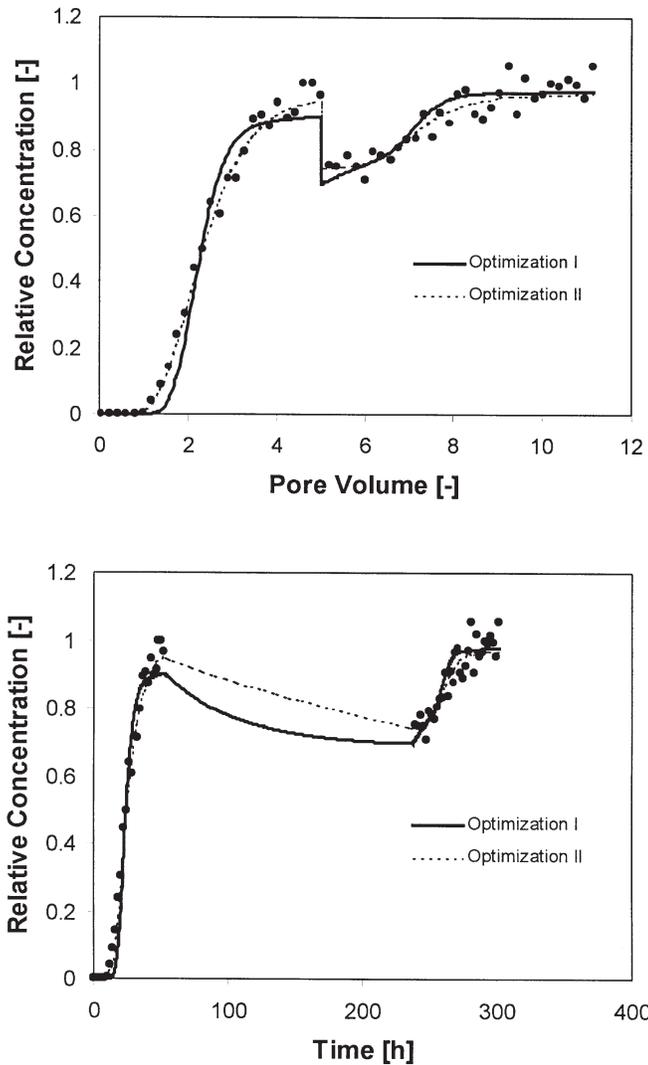


Fig. 6.6-2. Measured and optimized simazine breakthrough curves (vs. pore volume and real time) obtained using the flow interruption technique. Optimization I uses dispersivity estimated from the bromide effluent data; Optimization II fits dispersivity independently (data taken from Fortin et al., 1997).

sumed that, under the experimental conditions, the sorption isotherm for simazine is linear (Fortin et al., 1997). Figure 6.6-2 shows relative concentration values (vs. pore volume and in real time) of the two-site sorption model fitted to the measured simazine breakthrough curve. The fitted simulation (Optimization I) shows a reasonable representation of the simazine breakthrough for the final solute transport parameters ($k_d = 0.814 \pm 0.062 \text{ cm}^3 \text{ g}^{-1}$, $f = 0.533 \pm 0.046$, and $\alpha_{mt} = 0.0121 \pm 0.0044 \text{ h}^{-1}$). Correlation coefficients, r^2 , among optimized parameters were below 0.7. Note, however, that the spreading of the breakthrough curve is not very well captured by

the model simulation. Figure 6.6–2 also shows results (Optimization II) when four solute transport parameters, including dispersivity, were optimized ($\lambda = 1.08 \pm 0.246$ cm, $k_d = 1.49 \pm 2.57$ cm³ g⁻¹, $f = 0.328 \pm 0.564$, and $\alpha_{mt} = 0.00128 \pm 0.00406$ h⁻¹). The data are much better represented by Optimization II; however, the increased number of fitting parameters resulted in very high correlation coefficients among k_d , f , and α_{mt} ($r^2 = \pm 0.99$), indicating low confidence of these parameters (large confidence intervals). More details on the parameter optimization using this two-site two-rate model can be found in Fortin et al. (1997), but the general procedures of the parameter estimation are identical as employed in the example presented here.

6.6.3.3 Transient Laboratory Experiment with Equilibrium Solute Transport

The third example demonstrates the simultaneous estimation of soil hydraulic and solute transport parameters from a column infiltration experiment in a 30-cm-long and 5-cm-i.d. laboratory soil column (Inoue et al., 2000), containing a repacked coarse-textured soil (Tottori sand). The infiltration experiment was carried out by simultaneously increasing the solute concentration (from 0.02 to 0.1 mol L⁻¹ NaCl) and the infiltration rate (from 0.00032 to 0.0026 cm s⁻¹). Matric pressure heads, h , and bulk soil electrical conductivities, σ_a , were measured using automated minitensiometer and four-electrode sensors, respectively, at the 23-cm depth. The measured bulk soil electrical conductivity is a variable that integrates information on both water flow and solute transport, and can thus be beneficially used to simultaneously estimate soil hydraulic and solute transport parameters.

The soil hydraulic (van Genuchten, 1980) and solute transport parameters were estimated both sequentially and simultaneously. The objective function for the sequential optimization was defined first in terms of pressure heads to estimate soil hydraulic parameters (θ_r , θ_s , K_s , n , α , l ; Section 3.3.4) and then in terms of electrical conductivities to estimate solute transport parameters (λ). For the simultaneous optimization of both soil hydraulic and solute transport parameters, the objective function was defined in terms of both measured pressure heads and electrical conductivities. The results for the sequential optimization are shown in Fig. 6.6–3. It is specifically noted that the bulk electrical conductivity data show two separate fronts, demonstrating that water and solute fronts travel at different velocities depending on the ratio of initial and final water content values. Figure 6.6–3 also shows excellent correspondence between both optimized and measured pressure head and electrical conductivity values.

The sequentially estimated soil hydraulic and solute transport parameters (Table 6.6–1) were compared with independently measured solute dispersion (Fig. 6.6–4), soil water retention, and unsaturated hydraulic conductivity (Fig. 6.6–5) data. Notice from Table 6.6–1, that although the final parameter estimates for both sequential and simultaneous optimizations are very similar, the confidence intervals for the simultaneous optimization of soil hydraulic and solute transport parameters, as well as the final value of the objective function, are smaller. Dispersion coefficients (data points in Fig. 6.6–4) were obtained independently by fitting breakthrough curves derived from steady-state water flow column experiments (Inoue et al., 2000). The retention data of Fig. 6.6–5 were obtained from an additional in-

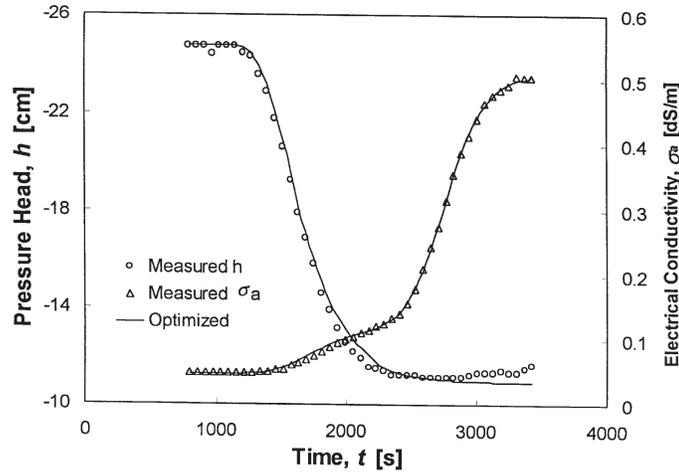


Fig. 6.6-3. Measured and optimized pressure heads and bulk electrical conductivities for a column infiltration experiment (data taken from Inoue et al., 2000).

Table 6.6-1. Soil hydraulic and solute transport parameters and their confidence intervals obtained using sequential and simultaneous optimizations.

Parameter	Sequential optimization	Simultaneous optimization
θ_r ($\text{cm}^3 \text{cm}^{-3}$)	0.0265 ± 0.0286	0.0206 ± 0.0198
θ_s ($\text{cm}^3 \text{cm}^{-3}$)	0.310 ± 0.0386	0.310 ± 0.0248
K_s (cm s^{-1})	0.138 ± 0.038	0.137 ± 0.024
n (-)	2.014 ± 0.318	1.969 ± 0.186
α (cm^{-1})	0.0446 ± 0.0388	0.0570 ± 0.0322
l (-)	-1.15 ± 0.178	-0.816 ± 0.220
λ (cm)	0.221 ± 0.024	0.207 ± 0.020
Φ	0.00347	0.00170

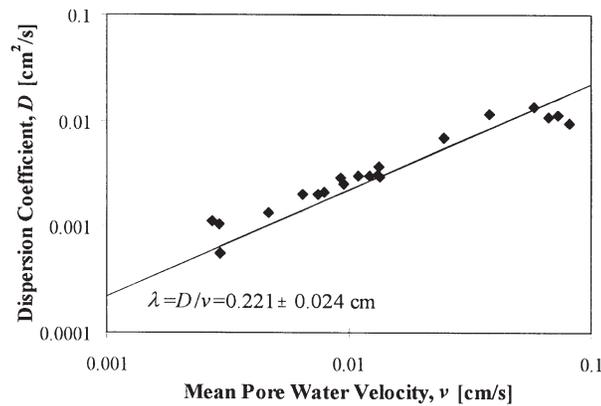


Fig. 6.6-4. Dispersion coefficient D as function of the mean pore water velocity v obtained by inverse optimization and from analysis of steady-state data (data taken from Inoue et al., 2000).

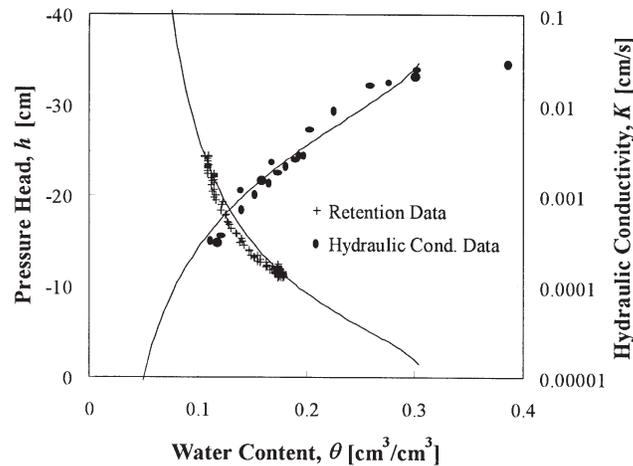


Fig. 6.6-5. Comparison between soil hydraulic properties estimated inversely (lines) and obtained from analysis of independent infiltration data (data points; data taken from Inoue et al., 2000).

filtration experiment in which the solute concentrations were kept constant, so that the measured electrical conductivities could be converted directly to water contents and related to the simultaneously measured pressure head values. The independent unsaturated hydraulic conductivity data were measured during steady-state experiments at different water flow rates. Correspondence between both optimized and independently measured soil hydraulic and dispersion properties is very good within the experimental range (Fig. 6.6-4 and 6.6-5, respectively). Further details about the above-described experiment, including calibration of the four-electrode probe, are given in Inoue et al. (2000).

6.6.3.4 Field Experiment with Nonequilibrium Solute Transport

The fourth example uses data collected during an elaborate field experiment that involved atmospheric boundary conditions, a layered soil profile, and nonequilibrium solute transport (Jacques et al., 2001). The soil hydraulic and solute transport parameters for individual soil layers were obtained sequentially. This example considers nonequilibrium solute transport using the mobile-immobile dual porosity concept.

Measured data were obtained from a 5.5-m-long and 1.2-m-deep transect located at Bekkevoort, Belgium (Jacques et al., 2001). Water contents and resident concentrations were measured laterally each 50 cm at five depths (15, 35, 55, 75, and 95 cm) using two-rod time domain reflectometry (TDR) probes (25 cm long, 0.5-cm rod diameter, 2.5-cm rod spacing). Matric pressure head values were measured using porous cups (6-mm diameter, 25 mm long) located at a horizontal distance of 10 cm from each TDR probe. TDRs and pressure transducers calibration procedures are described in Jacques et al. (2000).

The soil profile was described as having four horizons: Ap (0–25 cm), C1 (25–55 cm), and C2 (55–100 cm) overlying a Bt horizon. A thin layer of gravel was

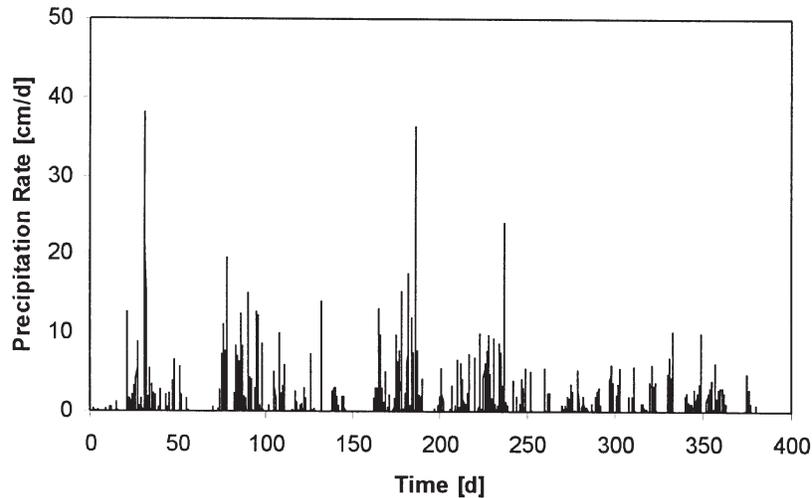


Fig. 6.6-6. Hourly precipitation rates during the Bekkevoort field experiment.

spread over the soil surface to minimize evaporation, prevent erosive effects by raindrops, and decrease weed growth. The soil surface was exposed to the atmosphere (Fig. 6.6-6). The tracer (CaCl_2) was applied on 28 Aug. 1998 in three pulses at a concentration of 75 g L^{-1} .

Field-averaged water contents, pressure heads, and resident concentrations were calculated for each depth by averaging measurements at particular depths. Resident concentrations were normalized as follows:

$$c^{r*}(z_i, t) = \frac{\theta(z_i, t)c^r(z_i, t)}{\int_0^t \theta(z_i, t)c^r(z_i, t)dt} \quad [6.6-11]$$

where $\theta(z_i, t)$ is the average water content at depth z_i and time t , $c^r(z_i, t)$ is the corresponding average resident solute concentration, and $c^{r*}(z_i, t)$ is the time-integral-normalized resident concentration (Vanderborght et al., 1996). Only four daily observations for each variable were used in the optimization. Data for 384 d were used in numerical simulations of water flow (11 Mar. 1998–30 Mar. 1999). Observations between Day 160 and 384, with solute applied on Day 168.5, were used for combined water flow and solute transport simulations. The layered soil profile was divided into four different horizons (0–15, 15–35, 35–55, and 55–150 cm, corresponding with the measurement depths), with layer-specific hydraulic and transport properties.

The following procedure was followed in order to minimize problems of uniqueness in the optimized parameters. The soil hydraulic parameters were optimized sequentially for each layer starting with the top layer. First, we assumed that the soil profile was homogeneous and optimized the soil hydraulic parameters (van Genuchten, 1980) against depth-averaged water contents and pressure heads measured at the first depth. Next, we fixed the parameters of the first layer, defined a two-

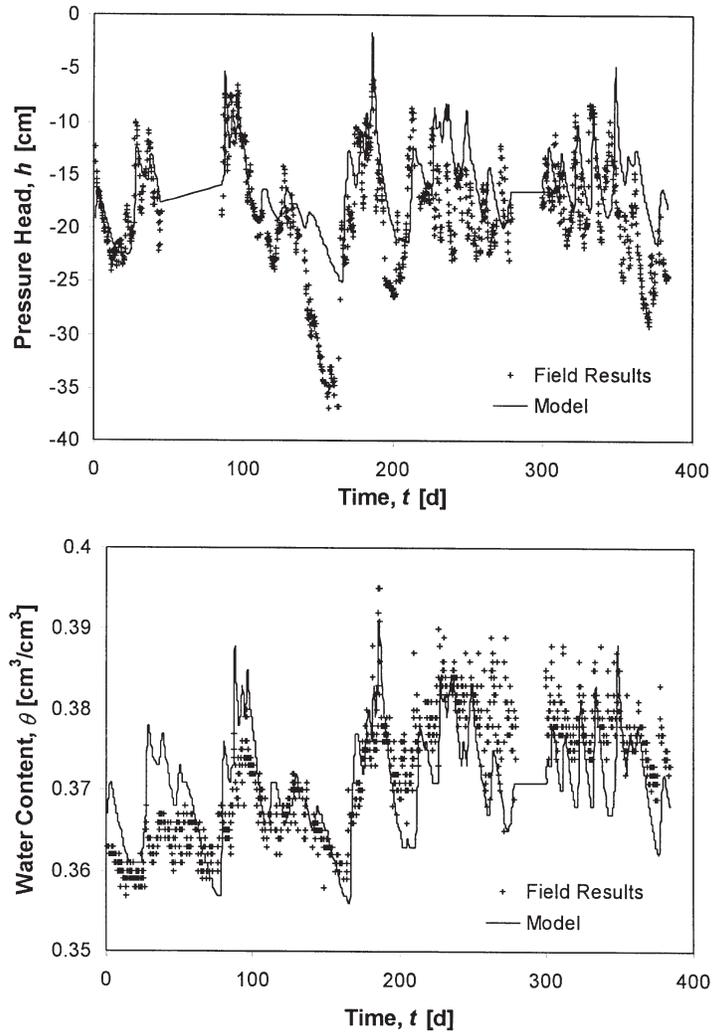


Fig. 6.6-7. Example of optimized pressure head and water content time series at a depth of 75 cm for the Bekkevoort field experiment (data taken from Jacques et al., 2001).

layer soil profile (0–15 and 15–150), and optimized parameters of the second layer against data from the second depth. Then a three-layer soil profile was defined, and parameters of the third layer were optimized and so on. A typical example of measured and optimized pressure head and water content time series is presented in Fig. 6.6-7 for the 75-cm depth.

Once a satisfying correspondence was obtained between measured and calculated water content and pressure head profiles, normalized resident concentrations (Eq. [6.6-11]) were used to optimize parameters for the physical nonequilibrium transport model, that is, the parameters θ_{im} (the immobile water content), λ (longitudinal dispersivity), and α'_{mt} (mass transfer coefficient). A similar proce-

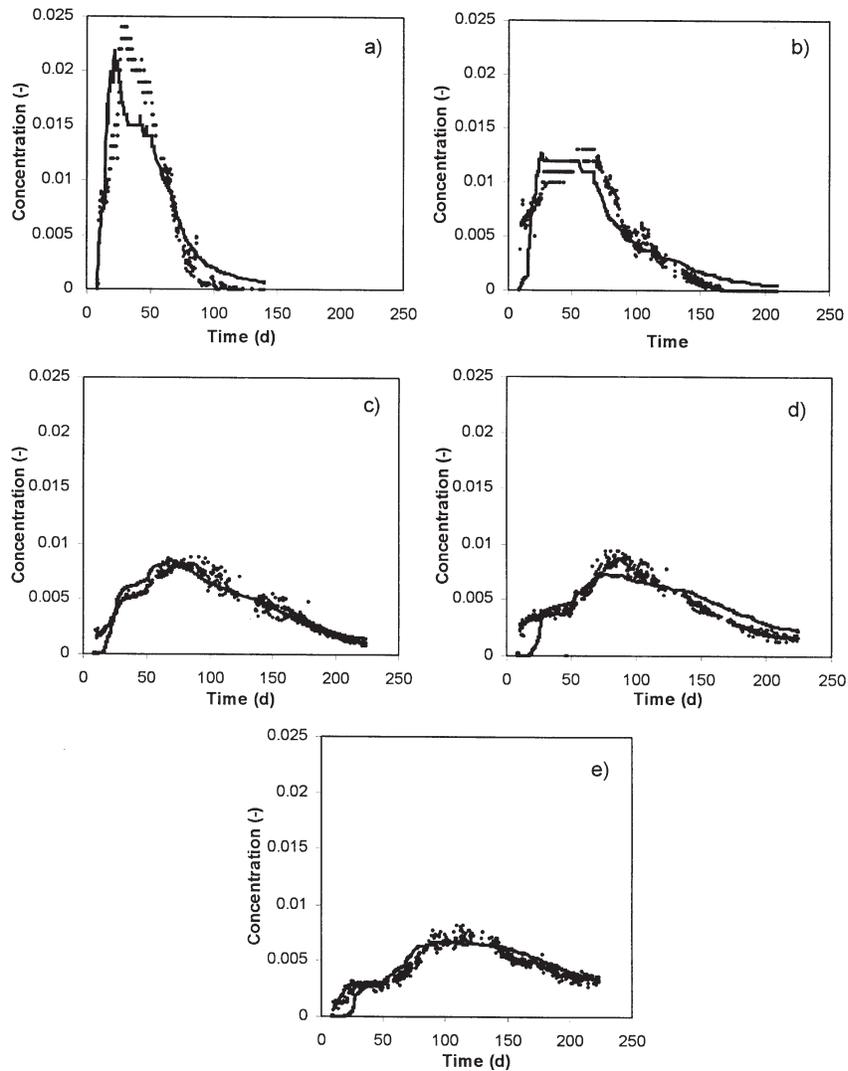


Fig. 6.6–8. Measured and optimized normalized resident concentrations at depths of (a) 15 cm, (b) 35 cm, (c) 55 cm, (d) 75 cm, and (e) 95 cm for the Bekkevoort field experiment (data taken from Jacques et al., 2001).

ture as for water flow was subsequently followed also for solute transport. Measured and optimized normalized resident concentrations at five different depths are shown in Fig. 6.6–8, while the optimized parameters are given in Table 6.6–2. Notice that the nonequilibrium transport model was able to adequately describe concentrations at all five depths, including the early solute arrival and long tailing at deeper depths. Our calculations showed that a large part of the porous space did not contribute to solute transport, and that only between 5 and 12% of the pore space

Table 6.6–2. Optimized solute transport parameters for the Bekkevoort field experiments.

Layer	θ_s	θ_{im}	λ (cm)	$\alpha'_{mt}(d^{-1})$
1	0.378	0.32	0.1	0.035
2	0.371	0.32	6.8	0.080
3	0.370	0.26	6.0	0.014
4	0.391	0.26	14.6	0.043

was mobile. Also, notice from Table 6.6–2 that the dispersivity increased with depth and that some variations existed in the transfer coefficients of the various layers. Jacques et al. (2000, 2001) gives additional details about this field experiment and the invoked analyses.

6.6.4 Conclusions

As was also discussed in Sections 1.7 and 3.6.2, the parameter estimation methods coupled with comprehensive numerical models can provide extremely useful tools for analyzing experimental data that may not be evaluated optimally using conventional tools such as analytical solutions. Various numerical codes (e.g., HYDRUS-1D) have been developed for identifying, either simultaneously or sequentially, soil hydraulic and solute transport parameters from unsaturated flow and transport data in one-, two-, and quasi-three-dimensional porous media. We demonstrated the utility of such tools using four examples of increasing complexity. Because of their generality (in terms of the definition of the objective function, the possible combination of different boundary and initial conditions, and options for considering multilayered systems), these tools are very attractive for analyzing conveniently a broad range of steady-state and transient laboratory and field flow and transport experiments.

6.6.5 References

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