

Colloid-Facilitated Solute Transport in Variably Saturated Porous Media: Numerical Model and Experimental Verification

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ABSTRACT

Strongly sorbing chemicals (e.g., heavy metals, radionuclides, pharmaceuticals, and explosives) in porous media are associated predominantly with the solid phase, which is commonly assumed to be stationary. However, recent field- and laboratory-scale observations have shown that in the presence of mobile colloidal particles (e.g., microbes, humic substances, clays, and metal oxides), colloids can act as pollutant carriers and thus provide a rapid transport pathway for strongly sorbing contaminants. To address this problem, we developed a one-dimensional numerical model based on the HYDRUS-1D software package that incorporates mechanisms associated with colloid and colloid-facilitated solute transport in variably saturated porous media. The model accounts for transient variably saturated water flow, and for both colloid and solute movement due to advection, diffusion, and dispersion, as well as for solute movement facilitated by colloid transport. The colloid transport module additionally considers the processes of attachment/detachment to/from the solid phase and/or the air–water interface, straining, and/or size exclusion. Various blocking and depth dependent functions can be used to modify the attachment and straining coefficients. The solute transport module uses the concept of two-site sorption to describe nonequilibrium adsorption–desorption reactions to the solid phase. The module further assumes that contaminants can be sorbed onto surfaces of both deposited and mobile colloids, fully accounting for the dynamics of colloid movement between different phases. Application of the model is demonstrated using selected experimental data from published saturated column experiments, conducted to investigate the transport of Cd in the presence of *Bacillus subtilis* spores in alluvial gravel aquifer media. Numerical results simulating bacteria transport, as well as the bacteria-facilitated Cd transport, are compared with experimental results. A sensitivity analysis of the model to various parameters is also presented.

COLLOIDAL PARTICLES (e.g., humic substances, clays, metal oxides, and microorganisms) are commonly found in subsurface environments (Kretzschmar et al., 1999). Many contaminants can sorb onto colloids in suspension, thereby increasing their concentrations in solution beyond thermodynamic solubilities (Kim et al., 1992). Experimental evidence now exists that many contaminants are transported not only in a dissolved state by water, but also sorbed to moving colloids. This colloid-facilitated transport has been illustrated in the literature for numerous contaminants, including heavy metals (Grolimund et al., 1996), radionuclides (Von Gunten

et al., 1988; Noell et al., 1998), pesticides (Vinten et al., 1983; Kan and Tomson, 1990; Lindqvist and Enfield, 1992), pharmaceuticals (Tolls, 2001; Thiele-Bruhn, 2003), hormones (Hanselman et al., 2003), and other contaminants (Magee et al., 1991; Mansfeldt et al., 2004). Since mobile colloids often move at rates similar or faster as nonsorbing tracers, the potential of enhanced transport of colloid-associated contaminants can be very significant (e.g., McCarthy and Zachara, 1989). Failure to account for colloid-facilitated solute transport can severely underestimate the transport potential and risk assessment for these contaminants. Models that can accurately describe the various mechanisms controlling colloid and solute transport, and their mutual interactions and interactions with the solid phase, are essential for improving predictions of colloid-facilitated transport of solutes in variably saturated porous media.

The transport behavior of dissolved contaminant species has been studied for many years. By comparison, colloid transport and the mutual interactions among contaminants, colloids, and porous media are less well understood. While colloids are subject to similar subsurface fate and transport processes as chemical compounds, they are also subject to their own unique complexities (van Genuchten and Šimůnek, 2004). Since many colloids and microbes are negatively charged, they are electrostatically repelled by negatively-charged solid surfaces. This will lead to an anion exclusion process that can cause slightly enhanced transport relative to fluid flow. The advective transport of colloids may similarly be enhanced by size exclusion, which limits their presence to the larger pores (Bradford et al., 2003, 2006). In addition to being subject to adsorption–desorption process at solid surfaces, colloids are also affected by straining in the porous matrix (Bradford et al., 2003, 2006) and may accumulate at air–water interfaces (Wan and Wilson, 1994; Thompson and Yates, 1999; Wan and Tokunaga, 2002). All of these additional complexities require colloid transport models to be more flexible than regular solute transport models.

Models that consider colloid-facilitated solute transport are based on mass balance equations for all colloid and contaminant species. The various colloid-facilitated solute transport models that have appeared in the literature differ primarily in the manner which colloid transport and contaminant interactions are handled. For example, Mills et al. (1991) and Dunnivant et al. (1992) assume that colloids are nonreactive with the solid phase, Corapcioglu and Jiang (1993) and Jiang and Corapcioglu (1993) consider a first-order kinetic attachment of colloids, Saiers and Hornberger (1996) consider an irreversible nonlinear kinetic attachment of colloids, and van de Weerd and Leijnse (1997) describe colloid attachment kinetics using the Langmuir equation. All colloid-facilitated transport models account for interactions be-

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tween the contaminants and colloids. Various equilibrium and kinetic models have been used for this purpose.

Although already relatively complex, no existing model for colloid-facilitated solute transport to our knowledge includes all of the major processes contributing to colloid and colloid-facilitated solute transport. For example, the majority of models for colloid-facilitated solute transport consider flow and transport only in fully saturated groundwater systems, usually for steady-state flow, and thus do not account for colloid interactions with the air–water interface. Also, no colloid-facilitated transport model has considered straining and size exclusion as mechanisms of colloid retention and transport, respectively. These two processes, and especially straining, have recently received much attention since classical colloid transport models are often unable to describe simultaneously both breakthrough curves vs. time and concentration profiles vs. depth (Bradford et al., 2003, 2006; Li et al., 2004; Tufenkji and Elimelech, 2005).

Straining involves the entrapment of colloids in down-gradient pores that are too small to allow particle passage. The critical pore size for straining will depend on the size of the colloid and the pore-size distribution of the medium (McDowell-Boyer et al., 1986; Bradford et al., 2002, 2003). Straining may have significant implications for colloid-facilitated solute transport, as illustrated by Bradford et al. (2006). Considering average capillary pressure-saturation curves for the 12 major soil textural groups given by Carsel and Parrish (1988), they calculated that a 2 μm colloid, which is the size of a clay particle, will be excluded or strained in 10 to 86% of the soil pore space for the various soil textures (Bradford et al., 2006). These percentages should significantly increase if the soils become unsaturated.

Size exclusion, a process closely related to straining, affects the mobility of colloids by constraining them to flow domains and pore networks that are physically accessible (Ryan and Elimelech, 1996; Ginn, 2002). Electrostatic forces also play an important role in the distribution (and mobility) of colloids. Anionic colloids will be excluded from locations adjacent to negatively charged solid surfaces; similar to the much reported anion exclusion process for anionic solutes (Krupp, 1972; Gvirtzman and Gorelick, 1991; Ginn, 1995). In case of size or anion exclusion, colloids will tend to reside in larger pores and in more conductive parts of the flow domain. As a result, colloids will be transported faster than a conservative solute tracer (Reimus, 1995; Cumbie and McKay, 1999; Harter et al., 2000; Bradford et al., 2004). Differences in the dispersive flux for colloids and a conservative solute tracer are also anticipated as a result of exclusion (Scheibe and Wood, 2003). Bradford et al. (2002) observed that the dispersivity of 3.2 μm carboxyl latex colloids was up to seven times greater than bromide in saturated aquifer sand. Conversely, Sinton et al. (2000) found in a field microbial transport experiment that the apparent colloid dispersivity decreased with increasing particle size.

Colloid and colloid-facilitated contaminant transport in partially saturated porous media is even more complex than in water-saturated systems. In addition to all of the processes and difficulties discussed above, colloid trans-

port in partially saturated porous media is further complicated by the presence of an air phase and thin water films, in addition to the solid and water phases present in saturated media. Wan and Wilson (1994) observed that colloidal particles deposit preferentially on the air–water interface via a capillary force acting on the particles, and that particle transport was tremendously retarded since the air–water interface acted as a strong sorption phase. Another physical restriction on colloid transport in unsaturated systems is imposed by thin water films; this process is often referred to as film straining (Wan and Tokunaga, 1997; Saiers and Lenhart, 2003). Wan and Tokunaga (1997) proposed that colloid transport in unsaturated systems depends on the ratio of the colloid size to water film thickness. Corapcioglu and Choi (1996) developed a mathematical model describing colloid transport in unsaturated porous media, and also studied the effect of colloids on volatile contaminant transport and air–water partitioning in unsaturated porous media.

Most current models for colloid-facilitated solute transport assume that the number of colloids with respect to contaminant is large and that kinetic reactions coefficients are not dependent on the number of colloids in the system. Although this may be true for some systems, the number of colloids (or concentrations) is often highly variable, with colloids being mobilized (or immobilized) due to changing chemical or hydrological conditions. Thus the reaction coefficients need to be adjusted to the number of colloids in the system in different phases (i.e., mobile, immobile, attached to the air–water interface). This adjustment needs to be performed also for numerical stability reasons. For example, if the number of colloids in the system decreases dramatically and the sorption constants for solute to colloids are assumed to be constant, this may lead to large sorbed concentrations, and hence numerical instabilities.

In this study we developed a one-dimensional numerical model based on the HYDRUS-1D software package that incorporates processes associated with colloid and colloid-facilitated solute transport in variably saturated porous media. The model accounts for both colloid and solute movement due to advection, diffusion, and dispersion in variably saturated soils, as well as for solute movement facilitated by colloid transport. The colloid transport module additionally considers the processes of attachment/detachment to/from the solid phase and/or the air–water interface, straining, and/or size exclusion. The model allows for different pore water velocities and dispersivities for colloids and solute. In this paper we first present the model itself, provide information about the numerical techniques used to solve the governing equations, and provide a simple application of the model to laboratory data. We also present a brief sensitivity analysis of the model to selected transport and reaction parameters.

CONCEPTUAL MODEL

The conceptual model of colloid and colloid facilitated solute transport (Fig. 1) is based on several assumptions. We assume that the porous medium consists of three phases, that is, solid phase, air, and water. Ac-

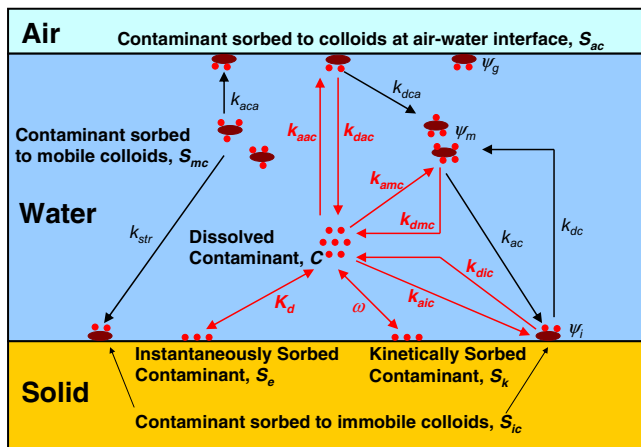
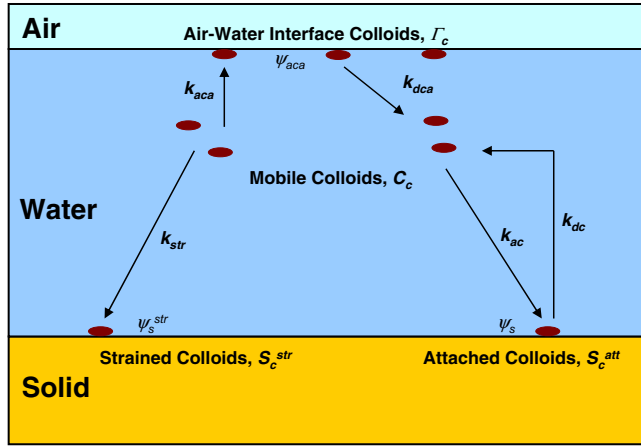


Fig. 1. Schematic of the (top) colloid transport and (bottom) colloid-facilitated solute transport model.

According to van de Weerd and Leijnse (1997), it is assumed that (a) only one type of colloids exists in the system that these colloids can be described by their mean behavior, (b) colloids are stable and that their mutual interactions in the liquid phase may be neglected, (c) immobile colloids do not affect the flow and transport properties of the porous medium because of their clogging of small pores, and (d) the transport of colloids is not affected by sorption of contaminants on colloids. We further assume that colloids exist in four states: mobile (suspended in water), attached to the solid phase, strained by the solid phase, and attached to the air-water interface (Fig. 1 top, Table 1). We further assume that colloid phase changes can be described using nonlinear first-order processes.

We further assume that contaminants can be dissolved in the liquid phase, as well as sorbed instantaneously and kinetically to the solid phase, and to colloids in all of their states. We thus distinguish six different states of contaminants (Fig. 1 bottom; Table 1): dissolved, instantaneously or kinetically sorbed to the solid phase, sorbed to mobile or immobile colloids (either strained or/attached to the solid phase), and colloids attached to the air-water interface. The coefficients k in Fig. 1 (Table 2) represent various first-order attachment/detachment or sorption/desorption rates, the coefficients K_d and ω represent instantaneous

Table 1. Species considered in the colloid and colloid-facilitated solute transport model (L is the length unit, M is the mass unit, and n is the number of colloids).

Species description	Variable	Units
Colloid species		
Mobile colloids	C_c	$n L^{-3}$
Colloids attached to the solid phase	S_c^{att}	$n M^{-1}$
Strained colloids	S_c^{str}	$n M^{-1}$
Colloids attached to the air-water interface	Γ_c	$n L^{-2}$
Solute (contaminant) species		
Dissolved contaminant	C	$M L^{-3}$
Contaminant instantaneously sorbed to the solid phase	S_e	$M M^{-1}$
Contaminant kinetically sorbed to the solid phase	S_k	$M M^{-1}$
Contaminant sorbed to mobile colloids	S_{mc}	$M n^{-1}$
Contaminant sorbed to immobile colloids	S_{ic}	$M n^{-1}$
Contaminant sorbed to colloids attached to the air-water interface	S_{ac}	$M n^{-1}$

and kinetic solute sorption to the solid phase, respectively, while the factors ψ account for nonlinearity of the process.

MATHEMATICAL MODEL

Variably Saturated Water Flow

Transient one-dimensional variably saturated water flow in porous media is described using the Richards equation (Richards, 1931):

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial x} \left[K \left(\frac{\partial h}{\partial x} + \cos \alpha \right) \right] - S \quad [1]$$

where h is the water pressure head [L], θ is the volumetric water content [$L^3 L^{-3}$], t is time [T], x is the spatial coordinate [L] (positive upward), S is the sink term [$L^3 L^{-3} T^{-1}$], α is the angle between the flow direction and the vertical axis, and $K(h)$ is the unsaturated hydraulic conductivity function [$L T^{-1}$]. The soil hydraulic properties, that is, the retention curve $\theta(h)$ and the unsaturated hydraulic conductivity function $K(h)$ can be evaluated using, for example, the analytical model of van Genuchten (1980).

Table 2. Kinetic reactions considered in the colloid and colloid-facilitated solute transport model (T is the time unit).

Reaction description	Variable	Units
Colloid species		
Colloids attachment coefficient	k_{ac}	T^{-1}
Colloids detachment coefficient	k_{dc}	T^{-1}
Colloids straining coefficient	k_{str}	T^{-1}
Colloids attachment coefficient to the air-water interface	k_{aca}	T^{-1}
Colloids detachment coefficient from the air-water interface	k_{dca}	T^{-1}
Solute (contaminant) species		
Solute adsorption rate to mobile colloids	k_{amc}	T^{-1}
Solute desorption rate from mobile colloids	k_{dmc}	T^{-1}
Solute adsorption rate to immobile colloids	k_{aic}	T^{-1}
Solute desorption rate from immobile colloids	k_{dic}	T^{-1}
Solute adsorption rate to colloids at the air-water interface	k_{aac}	T^{-1}
Solute desorption rate from colloids at the air-water interface	k_{dac}	T^{-1}

Colloid Transport

Colloid fate and transport models are commonly based on some form of the advection–dispersion equation, but modified to account for colloid filtration (Harvey and Garabedian, 1991; Hornberger et al., 1992; Corapcioglu and Choi, 1996; Bradford et al., 2003). A more comprehensive equation for colloid transport describing both colloid/matrix and colloid/air–water interface mass partitioning in one-dimensional form is given by

$$\frac{\partial \theta_w C_c}{\partial t} + \rho \frac{\partial S_c}{\partial t} + \frac{\partial A_{aw} \Gamma_c}{\partial t} = \frac{\partial}{\partial x} \left(\theta_w D_c \frac{\partial C_c}{\partial x} \right) - \frac{\partial q_c C_c}{\partial x} + R_c \quad [2]$$

where C_c is the colloid concentration in the aqueous phase [$n L^{-3}$], S_c and Γ_c are colloid concentrations adsorbed to the solid phase [nm^{-1}] and air–water interface [$n L^{-2}$], respectively; θ_w is the volumetric water content accessible to colloids [$L^3 L^{-3}$] (due to ion or size exclusion, θ_w may be smaller than the total volumetric water content θ), D_c is the dispersion coefficient for colloids [$L^2 T^{-1}$], ρ is the bulk density [$M L^{-3}$], A_{aw} is the air–water interfacial area per unit volume [$L^2 L^{-3}$], q_c is the volumetric water flux density for colloids [$L T^{-1}$], while R_c represents various chemical and biological reactions [$n L^{-3} T^{-1}$]. The second and third terms on the left side of Eq. [2] represent colloid mass-transfer terms between the aqueous phase and the solid phase or the air–water interface [$n L^{-3} T^{-1}$], respectively. The first two terms on the right side of Eq. [2] represent the dispersive and advective colloid fluxes, respectively. The value of θ_w is defined as

$$\theta_w = \theta - \varepsilon \gamma \quad [3]$$

where ε is porosity (equal to the saturated water content, θ_s) [$L^3 L^{-3}$] and γ is the water saturation that is not accessible to mobile colloids [-] (Bradford et al., 2006). The volumetric water flux density for colloids, q_c , moving only in pores from which they are not excluded, can be calculated from the ratio of the relative hydraulic conductivity of the entire pore space (K_{rw}) to the relative hydraulic conductivity of the colloid-accessible pores (K_{rc})

$$q_c = q \frac{K_{rc}}{K_{rw}} \quad [4]$$

where q is the volumetric water flux density for water [$L T^{-1}$]. The relative hydraulic conductivity of the colloid-accessible pores, K_{rc} [-], can then be calculated using, for example, the pore-size distribution model of Burdine (1953) by adjusting its limits of integration to reflect water flow to straining sites (Bradford et al., 2003) as

$$K_{rc} = S_w^2 \frac{\int_{\gamma}^{S_w} \frac{dS_w}{[h(S_w)]^2}}{\int_0^{\gamma} \frac{dS_w}{[h(S_w)]^2}} \quad S_w > \gamma \quad [5]$$

where S_w is the soil water saturation [-].

Colloid mass transfer between the aqueous and solid phases is traditionally described using attachment–detachment models of the form:

$$\rho \frac{\partial S_c}{\partial t} = \theta_w \psi_s f_s k_{ac} C_c - \rho k_{dc} S_c - R_{sc} \quad [6]$$

where R_{sc} represents various chemical and biological reactions acting on colloids that are kinetically attached to the matrix [$n L^{-3} T^{-1}$], k_{ac} and k_{dc} are the first-order colloid attachment and detachment coefficients [T^{-1}], respectively, ψ_s is a dimensionless colloid retention function [-], and f_s is the fraction of the solid surface area that is available for attachment. The attachment coefficient is generally calculated using filtration theory (Logan et al., 1995), a quasi-empirical formulation in terms of the median grain diameter of the porous medium (often termed the collector), the pore-water velocity, and collector and collision (or sticking) efficiencies accounting for colloid removal due to diffusion, interception and gravitational sedimentation (Rajagopalan and Tien, 1976; Logan et al., 1995; Tufenkji and Elimelech, 2004). The first-order detachment coefficient in Eq. [6] accounts for colloid mobilization, presumably as affected by changes in pore-water chemistry (ionic strength, ionic composition, and pH) and physical perturbations in flow, including changes in the flow rate and the water content.

To simulate reductions in the attachment coefficient due to filling of favorable sorption sites, ψ_s is sometimes assumed to decrease with increasing colloid mass retention. Random sequential adsorption (Johnson and Elimelech, 1995) and Langmuirian dynamics (Adamczyk et al., 1994) equations have been proposed for ψ_s to describe this blocking phenomenon, with the latter equation given by:

$$\psi_s = 1 - \frac{S_c}{S_c^{\max}} \quad [7]$$

in which S_c^{\max} is the maximum solid-phase colloid concentration [$n M^{-1}$]. Conversely, enhanced colloid retention during porous-medium ripening can theoretically be described using a functional form of ψ_s that increases with increasing mass of retained colloids (Tien, 1989; Tien and Chiang, 1985; Deshpande and Shonnard, 1999). We refer to several recent studies (Ginn, 2002; DeNovio et al., 2004; Rockhold et al., 2004) for more detailed discussions of the attachment and detachment coefficients in Eq. [6].

The first term on the right side of Eq. [6] is multiplied by the fraction of the solid surface area, f_s , that is available for attachment. Since mobile colloids are due to size exclusion transported in only a fraction of the pore space ($S_w - \gamma$), only a portion of the solid surface area is accessible for attachment. The fraction of the solid surface area that is available for attachment can be estimated as (Bradford et al., 2006):

$$f_s = \frac{\int_{\gamma}^{S_w} h(S_w) dS_w}{\int_0^{\gamma} h(S_w) dS_w} \quad [8]$$

Notice that Eq. [6] lumps the effects of a variety of physical and chemical processes into a single attachment-coefficient parameter. The attachment coefficient in Eq. [6] has been found to depend strongly on water content, with attachment significantly increasing as the water content decreases. This has been attributed to a variety of processes, including interfacial attachment and film straining. Bradford et al. (2002, 2003, 2006) hypothesized that the influence of straining and attachment mechanisms on colloid retention should be separated into two distinct components: attachment and detachment per se, and straining (being the entrapment of colloids in pore throats that are too small to allow passage). They modeled the influence of straining using an irreversible first-order expression as follows:

$$\rho \frac{\partial S_c}{\partial t} = \rho \frac{\partial S_c^{\text{str}}}{\partial t} + \rho \frac{\partial S_c^{\text{att}}}{\partial t} = \theta_w \psi_s^{\text{str}} k_{\text{str}} C_c + (\theta_w \psi_s f_s k_{\text{ac}} C_c - \rho k_{\text{dc}} S_c) - R_{\text{sc}} \quad [9]$$

where k_{str} is the first-order straining coefficient [T^{-1}], and S_c^{str} and S_c^{att} are the solid-phase concentrations of strained and attached colloids [$n M^{-1}$], respectively. The first term on the right-hand side of the above equation now accounts for straining and the second term (in parentheses) for attachment–detachment.

Application of the first-order attachment–detachment model given by Eq. [6] typically leads to exponential colloid distributions vs. depth. Bradford et al. (2003) showed that such exponential distributions are often inconsistent with experimental data. They obtained much better results using a depth-dependent straining coefficient ψ_s^{str} in Eq. [9] of the form

$$\psi_s^{\text{str}} = \left(\frac{d_{50} + x}{d_{50}} \right)^{-\beta} \quad [10]$$

where d_{50} is the median grain size of the porous media [L], β is a fitting parameter [-], and x is distance from the porous-medium inlet [L]. Data from Bradford et al. (2002, 2003) for different colloid diameters (d_p) and porous media median grain sizes showed an optimal value of 0.43 for β , while k_{str} could be described using a unique increasing function of the ratio of d_p/d_{50} . Subsequent studies with layered soils (Bradford et al., 2004) showed the importance of straining at and close to textural interfaces when flow occurs in the direction of coarse-textured to medium- and fine-textured media. Straining was found to be a significant mechanism for colloid retention for values of d_p/d_{50} greater than 0.005.

Finally, a model similar to Eq. [6] may be used to describe the partitioning of colloids to the air–water interface

$$\frac{\partial A_{\text{aw}} \Gamma_c}{\partial t} = \theta_w \psi_{\text{aca}} f_a k_{\text{aca}} C_c - A_{\text{aw}} k_{\text{dca}} \Gamma_c - R_{\text{aca}} \quad [11]$$

where Γ_c is the colloid concentration adsorbed to the air–water interface [$n L^{-2}$], R_{aca} represents various chemical and biological reactions of attached colloids to the air–water interface [$n L^{-3} T^{-1}$], A_{aw} is the air–water interfacial area per unit volume [$L^2 L^{-3}$], ψ_{aca} is a dimensionless colloid retention function for the air–water interface [-] similarly as used in Eq. [6], and f_a is the fraction of the air–water interfacial area that is available

for attachment [-], and k_{aca} and k_{dca} are the first-order colloid attachment and detachment coefficients to/from the air–water interface [T^{-1}], respectively. The interfacial area model of Bradford and Leij (1997) can be used to estimate the air–water interfacial area A_{aw} as:

$$A_{\text{aw}} = - \frac{\varepsilon}{\sigma_{\text{aw}}} \int_1^{S_w} P_{\text{aw}}(S) dS = \frac{\varepsilon \rho_w g}{\sigma_{\text{aw}}} \int_1^1 h(S) dS \quad [12]$$

where ε is the porosity [$L^3 L^{-3}$], P_{aw} and σ_{aw} are the air–water capillary pressure [$M L^{-1} T^{-2}$] and surface tension [$M T^{-2}$], respectively; h is the pressure head [L], ρ_w is the density of water [$M L^{-3}$], and g is the gravitational acceleration [$L T^{-2}$].

Colloid-Facilitated Solute Transport

Colloid-facilitated solute transport model requires knowledge of colloid transport, dissolved contaminant transport, and colloid-facilitated contaminant transport, and of various interactions between colloids, solute, soil, and air phase. Transport and/or mass-balance equations must therefore be formulated for the total contaminant, for contaminant sorbed kinetically or instantaneously to the solid phase, and for contaminant sorbed to mobile colloids, to colloids attached to the soil solid phase, and to colloids accumulated at the air–water interface, that is, for contaminant in all different phases or pools.

Our colloid-facilitated transport model closely follows development of many similar models (e.g., Corapcioglu and Jiang, 1993; Jiang and Corapcioglu, 1993; Saiers and Hornberger, 1996; van de Weerd and Leijnse, 1997; Bekhit and Hassan, 2005). Major differences in our model include consideration of water contents, water fluxes, and air–water interfacial areas that may change in time and space (i.e., transient variably-saturated water flow), the presence of colloids on the air–water interface, and adjustment of all kinetic rates to the number of colloids present in the system.

Mass-Balance Equation for the Total Contaminant

The combined dissolved and colloid-facilitated contaminant transport equation (in one dimension) is given by:

$$\begin{aligned} \frac{\partial \theta C}{\partial t} + \rho \frac{\partial S_c}{\partial t} + \rho \frac{\partial S_k}{\partial t} + \frac{\partial \theta_w C_c S_{\text{mc}}}{\partial t} + \rho \frac{\partial S_c S_{\text{ic}}}{\partial t} + \frac{\partial A_{\text{aw}} \Gamma_c S_{\text{ac}}}{\partial t} \\ = \frac{\partial}{\partial x} \left(\theta D \frac{\partial C}{\partial x} \right) - \frac{\partial q C}{\partial x} + \frac{\partial}{\partial x} \left(\theta_w S_{\text{mc}} D_c \frac{\partial C_c}{\partial x} \right) \\ - \frac{\partial q_c C_c S_{\text{mc}}}{\partial x} + R \end{aligned} \quad [13]$$

where C is the dissolved-contaminant concentration in the aqueous phase [$M L^{-3}$], S_c and S_k are contaminant concentrations sorbed instantaneously and kinetically, respectively, to the solid phase [$M M^{-1}$], S_{mc} , S_{ic} , and S_{ac} are contaminant concentrations sorbed to mobile and immobile (attached to solid and air–water interface) colloids [$M n^{-1}$], respectively; D is the dispersion coefficient for contaminants in solution [$L^2 T^{-1}$], q is the volumetric water density for the contaminant [$L T^{-1}$], and R represents various chemical and biological reac-

tions, such as degradation and production [$M L^{-3} T^{-1}$], discussed below. Note that the left-hand side sums the mass of contaminant associated with the different phases (contaminant in the liquid phase, contaminant sorbed instantaneously or kinetically to the solid phase, and contaminant sorbed to mobile colloids and immobile colloids attached to solid phase or air–water interface), while the right-hand side considers various spatial mass fluxes (dispersion and advective transport of the dissolved contaminant, as well as dispersion and advective transport of contaminant sorbed to mobile colloids) and sink/source reactions.

Mass-Balance Equation for Contaminant Sorbed to the Solid Phase

Eq. [13] invokes the concept of two-site sorption for modeling non-equilibrium adsorption–desorption reactions (e.g., van Genuchten and Wagenet, 1989). The two-site sorption concept assumes that total sorption, S , can be divided into two fractions:

$$S = S_e + S_k \quad [14]$$

with sorption S_e [$M M^{-1}$] on one fraction of the sites (type-1 sites) assumed to be instantaneous, and sorption S_k [$M M^{-1}$] on the remaining sites (type-2 sites) being time dependent according to

$$\rho \frac{\partial S_k}{\partial t} = \omega[(1-f)\Psi(C) - S_k] + R_{sk} \quad [15]$$

where ω is the first-order rate constant [T^{-1}], f is the fraction of exchange sites assumed to be in equilibrium with the solution phase [-], $\Psi(C)$ is the adsorption isotherm [$M M^{-1}$] that can be expressed using Freundlich, Langmuir, Freundlich–Langmuir, or linear adsorption models (Šimůnek et al., 1998), and R_{sk} represents various chemical and biological reactions of the kinetically sorbed contaminant [$M L^{-3} T^{-1}$].

Mass-Balance Equation for Contaminant Sorbed to Mobile Colloids

The mass-balance equation for contaminant sorbed to mobile colloids can be written as

$$\begin{aligned} \frac{\partial \theta_w C_c S_{mc}}{\partial t} = & \frac{\partial}{\partial x} \left(\theta_w S_{mc} D_c \frac{\partial C_c}{\partial x} \right) - \frac{\partial q_c C_c S_{mc}}{\partial x} + \theta \psi_m k_{amc} C \\ & - \theta_w k_{dmc} C_c S_{mc} - \theta_w (\psi_s f_s k_{ac} + \psi_{str} k_{str}) C_c S_{mc} \\ & + \rho k_{dc} S_c S_{ic} - \theta_w \psi_{aca} f_a k_{aca} C_c S_{mc} \\ & + A_{aw} k_{dca} \Gamma_c S_{ac} + R_{mc} \end{aligned} \quad [16]$$

where k_{amc} is the adsorption rate to mobile colloids [T^{-1}], k_{dmc} is the desorption rate from mobile colloids [T^{-1}], and R_{mc} represents various chemical and biological reactions for contaminant sorbed to mobile colloids [$M L^{-3} T^{-1}$]. The parameter ψ_m adjusts the sorption rate to the number of mobile colloids present, that is,

$$\psi_m = C_c / C_c^{ref} \quad [17]$$

where C_c^{ref} is the reference concentration of colloids for which the sorption rate k_{amc} is valid [$M L^{-3}$]. In Eq. [16],

the first two terms on the right-hand side represent dispersive and advective transport, respectively, of contaminant sorbed to mobile colloids; the third and fourth terms account for sorption and desorption of contaminants to/from mobile colloids, respectively; the fifth and sixth terms account for the attachment (including straining) and detachment of mobile colloids containing sorbed contaminants, respectively; the seventh and eighth terms account for the attachment and detachment of mobile colloids containing sorbed contaminants to/from air–water interface, respectively; while the ninth term represents degradation or other reactions involving contaminant sorbed to mobile colloids.

Mass-Balance Equation for Contaminant Sorbed to Immobile Colloids

The mass-balance equation for contaminant sorbed to immobile colloids can be written as follows

$$\begin{aligned} \rho \frac{\partial S_c S_{ic}}{\partial t} = & \theta \psi_i k_{aic} C - \rho k_{dic} S_c S_{ic} \\ & + \theta_w (\psi_s f_s k_{ac} + \psi_{str} k_{str}) C_c S_{mc} \\ & - \rho k_{dc} S_c S_{ic} + R_{ic} \end{aligned} \quad [18]$$

where k_{aic} is the adsorption rate to immobile colloids [T^{-1}], k_{dic} is the desorption rate from immobile colloids [T^{-1}], and R_{ic} represents various reactions for contaminant sorbed to immobile colloids [$M L^{-3} T^{-1}$]. The parameter ψ_i adjusts the sorption rate to the number of immobile colloids present:

$$\psi_i = S_c / S_c^{ref} \quad [19]$$

where S_c^{ref} is the reference concentration of immobile colloids for which the sorption rate k_{aic} is valid [nm^{-1}]. In Eq. [18] the first two terms on the right-hand side represent adsorption and desorption of contaminant to/from immobile colloids, respectively; the third and fourth terms describe the attachment (including straining) and detachment of immobile colloids with sorbed contaminant, respectively; and the fifth term represents reactions of contaminant sorbed to immobile colloids.

Mass-Balance Equation for Contaminant Sorbed to Colloids Attached to the Air–Water Interface

The mass-balance equation for contaminant sorbed to colloids attached to the air–water interface may be written as

$$\begin{aligned} \frac{\partial A_{aw} \Gamma_c S_{ac}}{\partial t} = & \theta \psi_g k_{aac} C - A_{aw} k_{dac} \Gamma_c S_{ac} \\ & + \theta_w \psi_{aca} f_a k_{aca} C_c S_{mc} - A_{aw} k_{dca} \Gamma_c S_{ac} + R_{ac} \end{aligned} \quad [20]$$

where k_{aac} is the adsorption rate to colloids at the air–water interface [T^{-1}], k_{dac} is the desorption rate from colloids at the air–water interface [T^{-1}], and R_{ac} represents various reactions for contaminant sorbed to colloids at the air–water interface [$M L^{-3} T^{-1}$]. Similarly as in Eq. [19], the parameter ψ_g adjusts the sorption rate to the number of colloids at the air–water interface:

$$\psi_g = \Gamma_c / \Gamma_c^{ref} \quad [21]$$

where Γ_c^{ref} is the reference concentration of immobile colloids for which sorption rate k_{aac} is valid [nL^{-2}]. In Eq. [20] the first two terms on the right-hand side represent the sorption and desorption, respectively, of contaminant to/from colloids at the air–water interface; the third and fourth terms account for the attachment and detachment, respectively, of colloids with sorbed contaminant to/from the air–water interface; whereas the fifth term represents degradation and other reactions of contaminant sorbed to colloids accumulated at the air–water interface.

Reaction Term

The reaction term R in Eq. [13] may be used to account for a variety of chemical and biological reactions and transformations, including degradation and production, not already explicitly incorporated in the main total contaminant mass transport equation. In the newly developed colloid-facilitated solute transport module we do not fully support current capabilities of the HYDRUS software package to simulate sequential first-order decay chains and can simulate transport of only one single compound. The reaction term R may thus include provisions for only one first-order degradation reaction that may have different rate coefficients in each phase (i.e., in the liquid, sorbed, and colloid phase). The reaction term R in Eq. [13] for colloid-facilitated transport scenarios is now given by:

$$R = -\mu_w \theta C - \mu_s \rho (S_k + S_e) - \mu_c (\theta_w C_c S_{\text{mc}} + \rho S_c S_{\text{ic}} + A_{\text{aw}} \Gamma_c S_{\text{ac}}) \quad [22]$$

where μ_w , μ_s , and μ_c are first-order rate constants [T^{-1}] for solutes in the liquid, solid, and colloid phases, respectively. Note that we assume that the solute degradation rate is the same for solute sorbed to all colloid, that is, mobile and immobile.

The terms R_{sk} , R_{mc} , R_{ic} , and R_{ac} for reactions in the kinetically sorbed phase, on mobile colloids and on colloids associated either with the solid phase or the air–water interface, respectively, are as follows:

$$\begin{aligned} R_{\text{sk}} &= -\mu_s \rho S_k \\ R_{\text{mc}} &= -\mu_c \theta_w C_c S_{\text{mc}} \\ R_{\text{ic}} &= -\mu_c \rho S_c S_{\text{ic}} \\ R_{\text{ac}} &= -\mu_c A_{\text{aw}} \Gamma_c S_{\text{ac}} \end{aligned} \quad [23]$$

SOLUTION OF THE GOVERNING EQUATIONS

The above mathematical development shows that a complete description of colloid-facilitated solute transport requires, in addition to variably-saturated flow equation, a total of nine coupled partial differential equations involving nine unknown variables (C_c , S_c^{str} , S_c^{att} , Γ_c , C , S_k , S_{mc} , S_{ic} , and S_{ac}). Four partial-differential equations pertain to four forms of colloids, that is, mobile colloids (C_c), strained colloids (S_c^{str}), attached colloids to the solid phase (S_c^{att}), and colloids attached to the air–water interface (Γ_c). Additional five partial-differential equations pertain to five forms of contami-

nants, that is, dissolved contaminant (C), contaminant kinetically sorbed to the solid phase (S_k), contaminant sorbed to mobile colloids (S_{mc}), contaminant sorbed to colloids associated with the solid phase (S_{ic}), and contaminant sorbed to colloids attached to the air–water interface (S_{ac}). Note that the instantaneously sorbed contaminant does not need a special partial differential equation, since it is described by the algebraic equation (adsorption isotherm) and treated simultaneously with the dissolved contaminant.

To find a solution for the flow Eq. [1] and the nine transport equations (Eq. [2], [6], [9], [11], [13], [15], [16], [18], and [20]) analytically is difficult, if not impossible. Numerical methods hence must be used to solve the flow and transport equations. Our numerical solution was implemented into the HYDRUS-1D software package (Šimůnek et al., 1998). The numerical solution is performed at each time step in three sequential steps.

First, because of the assumption that colloids do not affect the flow and transport properties of the porous medium, the variably-saturated flow Eq. [1] can be solved independently of the colloid and solute transport equations. Had we considered the effect of attached and strained colloids on the hydraulic conductivity (i.e., clogging), the soil hydraulic properties would have had to be updated at each time step depending on the number of strained and attached colloids. HYDRUS-1D uses a mass-lumped linear finite elements scheme for the spatial discretization and a fully implicit finite difference scheme for the temporal discretization (Šimůnek et al., 1998). The mixed form of the nonlinear Richards Eq. [1] was solved with a Picard iterative solution scheme. After achieving convergence, the nodal values of the fluid flux are determined from nodal values of the pressure head by applying Darcy's law, and together with nodal values of the water content subsequently used as input to the numerical solution of the colloid transport and colloid-facilitated solute transport equations.

Second, because of the assumption that the transport of colloids is not affected by sorption of contaminants on colloids, the four partial differential equations describing colloid transport can be solved independently of the five solute transport equations. The four governing equations (2, 6, 9, and 11) form a linear system when the dimensionless colloid retention functions ψ_s , ψ_s^{str} , and ψ_{aca} are equal to one (i.e., when blocking and depth-dependent phenomena are not considered). In that case, Eq. [6], [9], and [11], none of which contains spatial derivatives, are discretized using finite differences, similarly as for physical nonequilibrium solute transport in Šimůnek et al. (1998), and incorporated directly into the discretized form of Eq. [2]. The Galerkin finite element method (spatial discretization) coupled with the Crank–Nicholson finite difference method (temporal discretization) was used to solve the colloid transport Eq. [2] subject to appropriate initial and boundary conditions. When the dimensionless colloid retention functions ψ_s , ψ_s^{str} , and ψ_{aca} are not equal to one (i.e., when blocking or depth-dependent processes are considered), then the system of equations is nonlinear. For those cases we used a Picard iterative solution

scheme to solve the system of nonlinear equations. Again, after the solution of the colloid transport equations is obtained, nodal values of colloid concentrations in the different states (e.g., mobile, strained, and/or attached) are used as input to the numerical solution of the colloid-facilitated solute transport equations.

Finally, a Picard iterative solution scheme was used to solve the system of five equations describing colloid-facilitated solute transport (13, 15, 16, 18, and 20). We used again the finite element method for spatial discretization (of 13 and 15) and finite difference method for temporal discretization (of all five equations). After achieving convergence, and hence the solute concentrations of the different phases, the numerical solution can proceed to the next time step, starting again with the Richards equation.

MODEL VERIFICATION

We selected experimental data of Pang et al. (2005) to test our colloid- and colloid-facilitated solute transport model. In Pang et al. (2005), a column experiment was conducted to study the movement of Cd in the presence of *Bacillus subtilis* spores under saturated flow conditions. The column (18 cm long, 10 cm i.d.) was uniformly packed with coarse gravel aquifer material ($d_{50} = 16.69$ mm, $d_{60}/d_{10} = 53$), which gave bulk density of 1.9 g cm⁻³ and an effective porosity of 0.27. A solution (at fixed pH) containing approximately 4 mg L⁻¹ of Cd and 2 mg L⁻¹ of Br was first injected for about 1 h (5 pore-volumes). *Bacillus subtilis* spores were subsequently introduced to the column, along with Cd and Br, for another 40 min (3.4 pore-volumes). After that, the column was flushed with fresh water. A constant flow rate was applied during the entire experiment. Untreated groundwater extracted from alluvial gravel aquifers was used as the background electrolyte. Detailed information is given in Pang et al. (2005).

Figure 2 shows the observed breakthrough curves (BTCs) of Br, *B. subtilis* spores and Cd from the column experiment. Although Br and Cd solutes were injected simultaneously in the beginning of the experiment, the BTC of Cd showed a slow increase of concentrations com-

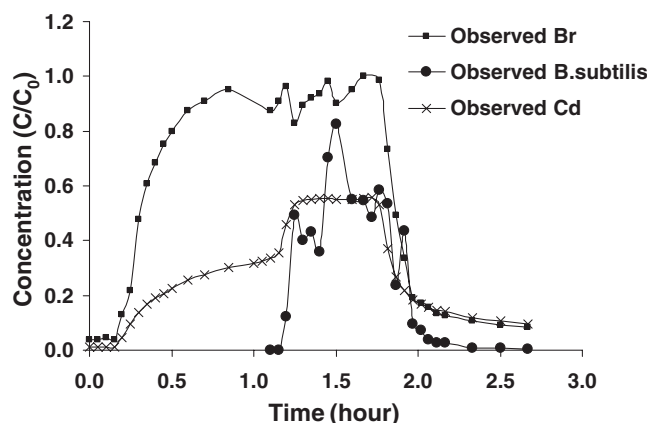


Fig. 2. Observed Br, *Bacillus subtilis* spores, and Cd breakthrough curves for the column experiment of Pang et al. (2005).

pared to the BTC of Br, which suggests a higher adsorption capability of Cd onto the solid matrix. After injection of the spores, a simultaneous steep rise and flat plateau of both *B. subtilis* spores and Cd occurred. This observation implies that Cd was co-transported with the spores.

The column experiment was simulated in three steps (Pang and Šimůnek, 2006). First, the Br breakthrough curve was used to optimize the pore-water velocity and longitudinal dispersivity. Next, the *B. subtilis* breakthrough curve was used to optimize the first-order attachment and detachment coefficients, while the pore-water velocity and longitudinal dispersivity were fixed at the values determined for Br. Finally, the Cd breakthrough curve was analyzed to obtain the distribution coefficient, the first-order rate constant for exchanging between two sorption sites, and the adsorption and desorption rate coefficients to/from immobile bacteria. Pang and Šimůnek (2006) independently determined adsorption and desorption rate coefficients to/from mobile bacteria from a batch kinetic study in the absence of aquifer media. Results of preliminary simulations suggest that almost all Cd sorption sites of the solid phase were kinetic. These rate coefficients, together with parameters for the bacteria and flow, were fixed during simulations of the Cd data. Parameters were optimized using the internal HYDRUS optimization routine (Marquardt, 1963) for the Br and bacteria data and the PEST software (Doherty, 1994) for the Cd data. The optimized parameters are given in Table 3, while a comparison of model-predicted results and observed experimental data is presented in Fig. 3. Notice an excellent correspondence between optimized and measured breakthrough curves for all three compounds. Since the column experiment was conducted under saturated condition, the simulation did not consider the attachment-detachment of colloids to/from the air-water interface. As we assumed the same pore-water velocity and dispersion for Br and the bacteria, size exclusion was also not considered here. Pang and Šimůnek (2006) provide more details about

Table 3. Transport and reaction parameters used to simulate the Br, *Bacillus subtilis* spores, and Cd breakthrough curves presented in Fig. 3.

Description	Parameter	Value
Br tracer parameters		
Saturated water content	θ_s	0.27
Saturated hydraulic conductivity, cm h ⁻¹	K_s	16.7
Bulk density, g cm ⁻³	ρ	1.9
Longitudinal dispersivity, cm	α_L	0.9
Saturation	S_w	1.0
Colloid (<i>Bacillus subtilis</i> spores) parameters		
First-order colloid attachment coefficient, h ⁻¹	k_{ac}	1.697
First-order colloid detachment coefficient, h ⁻¹	k_{dc}	0.0001
Water saturation that is not accessible to mobile colloids	γ	0
Solute (Cd) parameters		
Adsorption isotherm coefficient of Cd, cm ³ g ⁻¹	K_d	2.29
Cd adsorption rate to mobile colloids, h ⁻¹	k_{amc}	2.30†
Cd desorption rate from mobile colloids, h ⁻¹	k_{dmc}	1.28†
Cd adsorption rate to immobile colloids, h ⁻¹	k_{aic}	18.7
Cd desorption rate from immobile colloids, h ⁻¹	k_{dic}	0.00
Cd first-order rate constant for kinetic sorption, h ⁻¹	ω	0.25

† Independently determined from a batch kinetic study in the absence of aquifer media (Pang and Šimůnek, 2006).

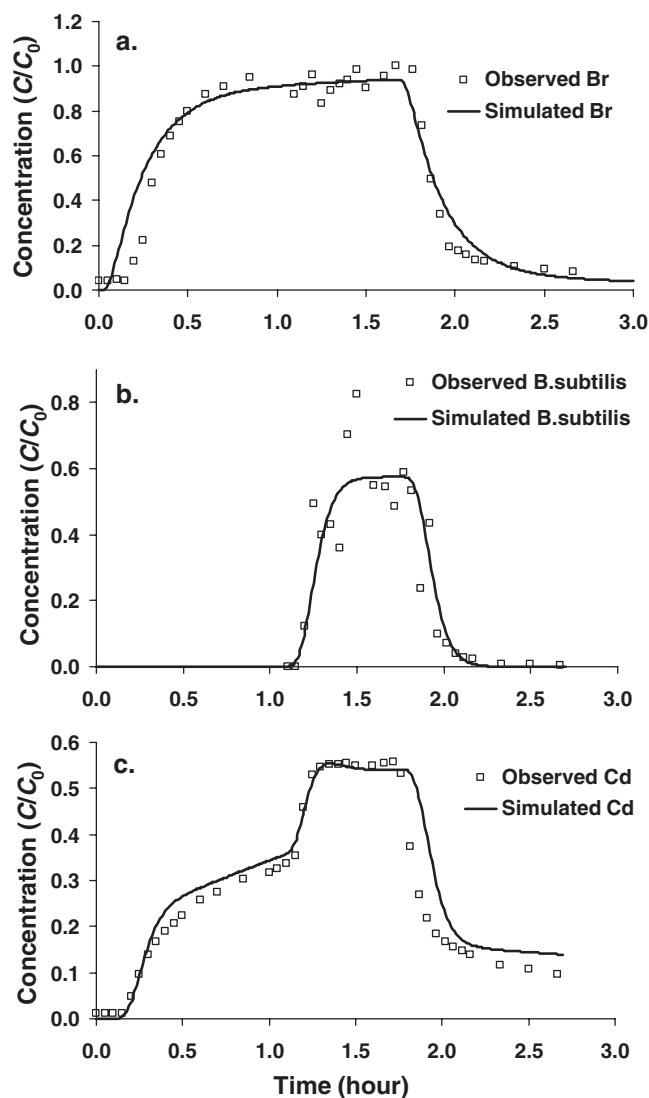


Fig. 3. (a) Observed and simulated Br, (b) *Bacillus subtilis* spores, and (c) Cd breakthrough curves for the column experiment of Pang et al. (2005).

the experimental set up, batch studies, as well as more examples of model experimental validation involving Cd transport with either *B. subtilis* spores or *Escherichia coli*.

SENSITIVITY ANALYSIS

A sensitivity analysis can be one of the most powerful uses of complex transport models. Such an analysis permits a systematic evaluation of the impact of various model parameters (both transport and reactive), and initial and boundary conditions on the model output. The results of a sensitivity analysis provide insight into the relative importance of individual reactions within a complex geochemical system. These results can thus help one to identify the most important parameters and processes, and thus help guide allocation of resources for laboratory and field investigations (Šimůnek and Valocchi, 2002).

In the sensitivity analysis here we assume that all physical properties, such as porosity, bulk density, water flux, dispersivity, and pore-water velocity are the same as for the column experiment discussed above for *B. subtilis* spores and Cd. Since the sensitivity of colloid BTCs to various parameters and processes, such as straining and size exclusion, was presented elsewhere (e.g., Bradford et al., 2003), we evaluate here only the sensitivity of model output to the various solute transport parameters.

In this section we evaluate the effects of the solute sorption coefficients on the solute BTC. The analysis considers the same properties for colloids as before (Table 4). We assume that the column is fully saturated and that all pores are accessible to colloids. We further assume that solute sorption to almost all sorption sites of the solid phase is kinetic ($f = 0.01$) and that the distribution coefficient K_d is equal to $2.5 \text{ cm}^3 \text{ g}^{-1}$ (and 0, 1, and 2.5 in the sensitivity analysis). The adsorption rate of contaminant to mobile colloids is considered to be equal to the adsorption rate to immobile colloids (i.e., $k_{amc} = k_{aic}$) and, similarly, the desorption rate from mobile colloids is assumed to be equal to the desorption rate from immobile colloids (i.e., $k_{dmc} = k_{dic}$). While colloids were applied during the time interval between 1 and 1.9 h, solute was applied between 0 and 1.9 h.

In the first analysis we assumed that both the adsorption and desorption coefficients were constant (i.e., $k_{amc} = k_{dmc} = 10 \text{ h}^{-1}$) and varied the solute distribution coefficient K_d from 0 (no retardation) to 1, and $2.5 \text{ cm}^3 \text{ g}^{-1}$. In the second analysis we kept constant $K_d (= 2.5 \text{ cm}^3 \text{ g}^{-1})$ and $k_{dmc} (= 1 \text{ h}^{-1})$ and changed the adsorption coefficient k_{amc} from 1 to 10, and 50 h^{-1} . Finally, in the last analysis, we kept constant $K_d (= 2.5 \text{ cm}^3 \text{ g}^{-1})$ and $k_{amc} (= 10 \text{ h}^{-1})$ values, but varied the value of k_{dmc} from 0.1 to 1, and 10 h^{-1} .

The colloid BTCs were the same in all three runs (Fig. 4). Figure 4 (top) shows additionally solute BTCs for three different values of K_d . Recall that almost all sorption sites are kinetic and thus that the distribution coefficient does not lead to a retardation of the solute

Table 4. Parameter values used in the sensitivity analysis of colloid and solute breakthrough curves evaluating effects of various solute sorption coefficients. Parameter values in parenthesis were used in alternative runs in the sensitivity analyses.

Description	Parameter	Value
Colloid parameters		
First-order colloid attachment coefficient, h^{-1}	k_{ac}	1.97
First-order colloid detachment coefficient, h^{-1}	k_{dc}	0.0001
Water saturation that is not accessible to mobile colloids	γ	0
Water saturation	S_w	1
Solute parameters		
Distribution coefficient, $\text{cm}^3 \text{ g}^{-1}$	K_d	2.5 (0, 1, 2.5)
Mass transfer coefficient, h^{-1}	ω	0.3
Fraction of exchange sites assumed to be in equilibrium with the solution phase	f	0.01
First-order attachment coefficient to mobile and immobile colloids, h^{-1}	k_{amc} k_{aic}	10 (1, 10, 50)
First-order detachment coefficient from mobile and immobile colloids, h^{-1}	k_{dmc} k_{dic}	10 (0.1, 1, 10)

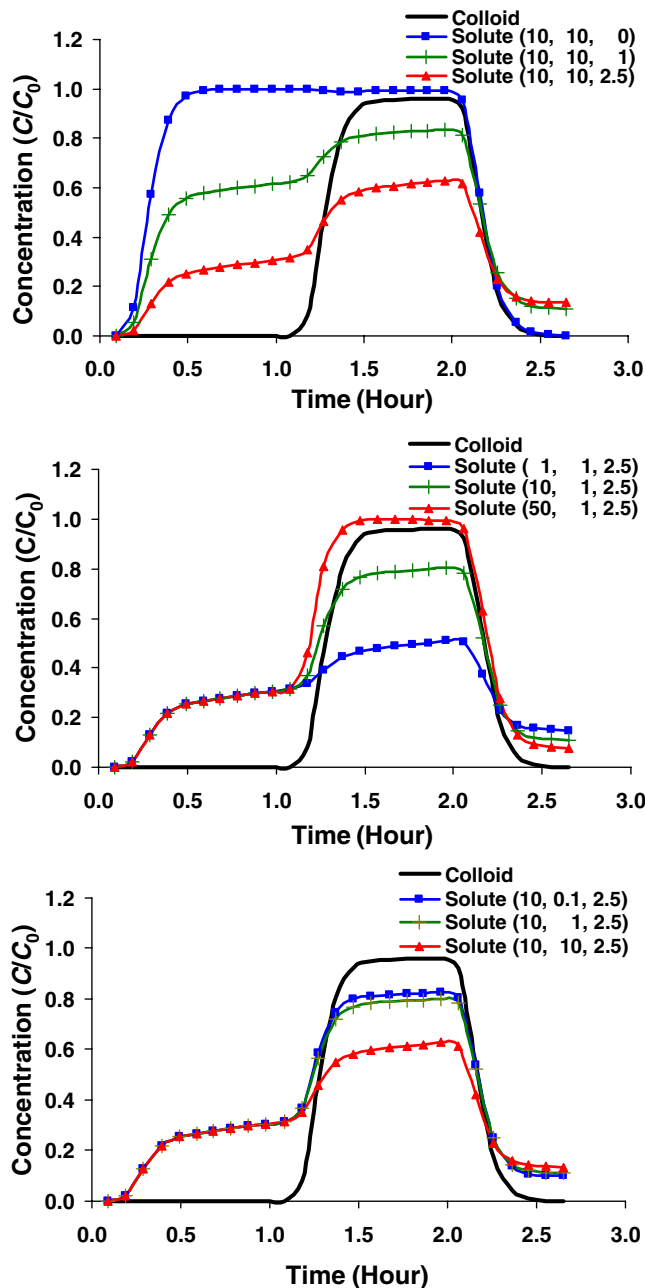


Fig. 4. Sensitivity of simulated breakthrough curves to the (top) distribution coefficient K_d ; (middle) adsorption coefficients to mobile and immobile colloids k_{amc} and k_{aic} , respectively; and (bottom) desorption coefficients from mobile and immobile colloids k_{dmc} and k_{dic} , respectively. The first position in parentheses in the legend represents k_{amc} and k_{aic} , the second k_{dmc} and k_{dic} , and the third K_d .

front. Kinetic adsorption to the solid phase leads to a gradual increase in solute concentration after arrival of the solute front, and an additional gradual increase in concentration after arrival of the colloid front. For the case of no adsorption to the solid phase (i.e., $K_d = 0$), solute concentrations quickly reached unit relative concentration after arrival of the solute front, and stayed at this level until the end of the solute pulse. Colloids did not have any effect on the solute breakthrough for this set of solute transport parameters since solute was not retarded and thus its transport cannot be ac-

celerated by colloids unless they are excluded from some part of the pore space and travel faster than unretarded solute. The effects of colloids on solute transport become apparent when solute is kinetically sorbed. Increasing the kinetic sorption coefficient of the solute produced a more pronounced effect of colloids on solute transport (Fig. 4, top).

A different picture is obtained when sorption to the solid phase is assumed constant ($K_d = 2.5 \text{ cm}^3 \text{ g}^{-1}$), but the adsorption coefficient to the colloids ($k_{amc} = k_{aic} = 1, 10, \text{ or } 50 \text{ h}^{-1}$) is varied. The initial phase of the solute concentration BTC was the same for all three runs (Fig. 4, middle) since all solute transport parameters characterizing interactions with the soil were the same. Dramatic changes occurred only after the arrival of colloids since sorption rates to the colloids were different for the three runs. The higher the adsorption rate to the colloids, the higher the peaks of the solute concentration BTC as a consequence of more solute arriving at the end of the column sorbed to mobile colloids.

Similar results were obtained when varying the desorption rates from the mobile and the immobile colloids ($k_{dmc} = k_{dic} = 0.1, 1, \text{ or } 10 \text{ h}^{-1}$). We obtained again the same initial phase of the solute concentration BTC for all three runs (Fig. 4, bottom). Then due to relatively high sorption to both mobile and immobile colloids, concentrations relatively quickly increased with arriving colloids. Due to different desorption rates from the colloids, the plateaus of the solute concentration BTCs were at different levels.

SUMMARY

We developed a one-dimensional numerical model based on the HYDRUS-1D software package that incorporates various processes associated with colloid and colloid-facilitated solute transport in variably saturated porous media. The numerical model accounts for transient variably saturated water flow and for both colloid and solute movement due to convection, diffusion, and dispersion, as well as for solute movement facilitated by colloid transport. The colloid transport module additionally considers the processes of attachment/detachment to/from the solid phase and/or the air-water interface. A unique feature of our colloid-facilitated solute transport model is that it accounts for size exclusion and depth-dependent straining.

The solute transport module uses the concept of two-site sorption to describe nonequilibrium adsorption-desorption reactions to the solid phase. The module further assumes that contaminants can be sorbed onto surfaces of both deposited and mobile colloids, thus fully accounting for the dynamics of colloid transfer between different phases. While a majority of models for colloid-facilitated solute transport assume that the number of colloids with respect to the contaminant is large and that kinetic reaction coefficients are not dependent on the number of colloids in the system, our newly developed model accounts for a variable number of colloids in the system; this since colloids may be mobilized (or immobilized) due to changing chemical or hydrological con-

ditions. Our model can also account for different transport velocities of colloids and solute due to the size exclusion of colloids from small pores.

The use of the model was demonstrated using experimental data from a saturated column experiment, conducted to investigate the transport of Cd in the presence of *Bacillus subtilis* spores. We also presented a brief sensitivity analysis of the model to selected reaction parameters characterizing various sorption and desorption coefficients.

Our future work will involve further verification of the code using experimental data derived for more complex conditions, such as transient water flow with mobilization and immobilization of colloids, with colloids interacting with the air–water interface and/or being excluded from part of the pore space.

APPENDIX: LIST OF VARIABLES

A_{aw}	air–water interfacial area per unit volume [$L^2 L^{-3}$]	R_{ic}	various reactions for contaminant sorbed to immobile colloids [$M L^{-3} T^{-1}$]
C	dissolved-contaminant concentration in the aqueous phase [$M L^{-3}$]	R_{mc}	various chemical and biological reactions for contaminant sorbed to mobile colloids [$M L^{-3} T^{-1}$]
C_c	colloid concentration in the aqueous phase [$n L^{-3}$]	R_{sc}	various chemical and biological reactions acting on kinetically attached colloids to the matrix [$n L^{-3} T^{-1}$]
C_c^{ref}	reference concentration of colloids for which the sorption rate k_{amc} is valid [$M L^{-3}$]	R_{sk}	various chemical and biological reactions of the kinetically sorbed contaminant [$M L^{-3} T^{-1}$]
d_{50}	median grain size of the porous media [L]	q	volumetric water density for the contaminant [$L T^{-1}$]
D	dispersion coefficient for contaminants in solution [$L^2 T^{-1}$]	q_c	volumetric water flux density for colloids [$L T^{-1}$]
D_c	dispersion coefficient for colloids [$L^2 T^{-1}$]	S	sink term [$L^3 L^{-3} T^{-1}$]
f	fraction of exchange sites assumed to be in equilibrium with the solution phase [-]	S_{ac}	contaminant concentration sorbed to immobile (attached to the air–water interface) colloids [$M n^{-1}$]
f_a	fraction of the air–water interfacial area that is available for attachment [-]	S_c	colloid concentrations adsorbed to the solid phase [$n M^{-1}$]
f_s	fraction of the solid surface area that is available for attachment [-]	S_c^{ref}	reference concentration of immobile colloids for which the sorption rate k_{aic} is valid [$n M^{-1}$]
g	gravitational acceleration [$L T^{-2}$]	S_c^{att}	solid-phase concentrations of attached colloids [$n M^{-1}$]
h	pressure head [L]	S_c^{max}	maximum solid-phase colloid concentration [$n M^{-1}$]
k_{aac}	first-order colloid attachment coefficient [T^{-1}]	S_c^{str}	solid-phase concentration of strained colloids [$n M^{-1}$]
k_{aac}	adsorption rate to colloids at the air–water interface [T^{-1}]	S_e	contaminant concentration sorbed instantaneously to the solid phase [$M M^{-1}$]
k_{aca}	first-order colloid attachment coefficient to the air–water interface [T^{-1}]	S_{ic}	contaminant concentration sorbed to immobile (attached to the solid phase) colloids [$M N^{-1}$]
k_{aic}	adsorption rate to immobile colloids [T^{-1}]	S_k	contaminant concentration sorbed kinetically to the solid phase [$M M^{-1}$]
k_{amc}	adsorption rate to mobile colloids [T^{-1}]	S_{mc}	contaminant concentration sorbed to mobile colloids [$M n^{-1}$]
k_{dc}	first-order colloid detachment coefficients [T^{-1}]	S_w	soil water saturation [-]
k_{dac}	desorption rate from colloids at the air–water interface [T^{-1}]	t	time [T]
k_{dca}	first-order colloid detachment coefficient from the air–water interface [T^{-1}]	x	spatial coordinate [L] (positive upward)
k_{dic}	desorption rate from immobile colloids [T^{-1}]	β	fitting parameter [-]
k_{dmc}	desorption rate from mobile colloids [T^{-1}]	γ	water saturation that is not accessible to mobile colloids [-]
k_{str}	first-order straining coefficient [T^{-1}]	Γ_c	colloid concentrations adsorbed to the air–water interface [$n L^{-2}$]
K	unsaturated hydraulic conductivity [LT^{-1}]	Γ_c^{ref}	reference concentration of immobile colloids for which sorption rate k_{aac} is valid [$n L^{-2}$]
K_{rc}	relative hydraulic conductivity of the colloid-accessible pores [-]	ε	porosity [$L^3 L^{-3}$]
K_{rw}	relative hydraulic conductivity of the entire pore space [-]	μ_c	first-order rate constant for solutes in the colloid phase [T^{-1}]
P_{aw}	air–water capillary pressure [$M L^{-1} T^{-2}$]	μ_s	first-order rate constant for solutes in the solid phase [T^{-1}]
R	various chemical and biological reactions, such as degradation and production, for contaminant [$M L^{-3} T^{-1}$]	μ_w	first-order rate constant for solutes in the liquid phase [T^{-1}]
R_{aca}	various chemical and biological reactions of attached colloids to the air–water interface [$n L^{-3} T^{-1}$]	ψ_{aca}	dimensionless colloid retention function for the air–water interface [-]
R_{ac}	various reactions for contaminant sorbed to colloids at the air–water interface [$M L^{-3} T^{-1}$]	ψ_g	parameter adjusting the sorption rate to the number of colloids at the air–water interface [-]
R_c	various chemical and biological reactions for colloids [$n L^{-3} T^{-1}$]	ψ_i	parameter adjusting the sorption rate to the number of immobile colloids present
		ψ_m	parameter adjusting the sorption rate to the number of mobile colloids present
		ψ_s	dimensionless colloid retention function [-]
		Ψ	(C) adsorption isotherm [$M M^{-1}$]
		ω	first-order rate constant [T^{-1}]
		σ_{aw}	air–water surface tension [$M T^{-2}$]
		θ	volumetric water content [$L^3 L^{-3}$]
		θ_w	volumetric water content accessible to colloids [$L^3 L^{-3}$]
		ρ	bulk density [$M L^{-3}$]
		ρ_w	density of water [$M L^{-3}$]

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