



Numerical Modeling of Vadose Zone Processes (with focus on **HYDRUS** Software Packages)

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(with contributions from)

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Outline

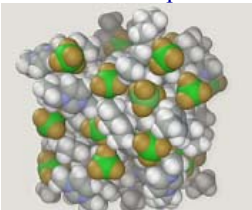
- ◆ **Modeling**
 - > Scientific Modeling
 - > Mathematical Modeling
 - > Numerical Modeling
 - > Modeling of Vadose Zone Processes
- ◆ **HYDRUS** Family of Models and Modules:

- HP1/HP2	- general biogeochemical module
- UnsatChem	- transport of major ions
- Wetland	- C and N processes
- DualPerm	- preferential flow and transport
- Fumigants	- transport of fumigants
- C-Ride	- colloid-facilitated solute transport

Modeling

The process of creating abstract or conceptual models

- ◆ **Sculpting** - to create a form from a substance such as clay
- ◆ **Fashion Modeling** - to display objects (clothing) for others to see
- ◆ **Molecular Modeling** - to mimic the behavior of molecules
- ◆ **Modeling Psychology** - a type of behavior learned through observation of others demonstrating the same behavior
- ◆ **Physical Models** - to make a miniature model of a technical artifact
- ◆ **Scientific Modeling** - the process of creating abstract or conceptual models and their use in the creation of predictive statements.

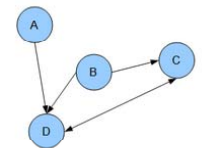


Scientific Modeling

Scientific Modeling is the process of generating various **abstract, physical, graphical, conceptual, and/or mathematical** models.

A **Scientific Model** is a **simplified** abstract view of a complex reality, in which empirical objects, phenomena, and physical processes are represented in a logical way by graphical objects, abstract ideas, or mathematical equations.

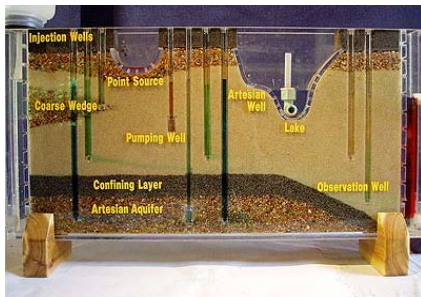
A **Graphical Model** is a probabilistic model, in which a graph denotes the conditional dependence structure between random variables.



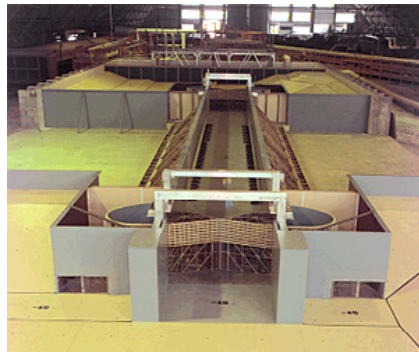
An example of a graphical model

Physical Models in Hydrology

Mostly used before the development and wide use of numerical hydrological models.



Example of a Physical Groundwater Model
Photo Credit: West Virginia Conservation Agency



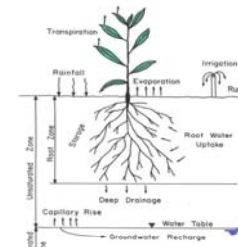
Dry bed view of Type 1 physical model looking from lakeside to riverside.

Conceptual Model

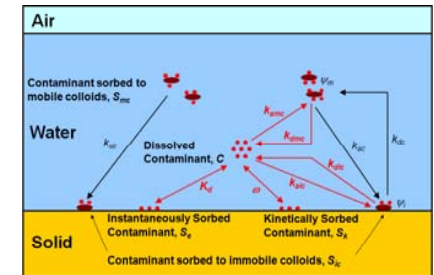
Conceptual Model - formed after a conceptualization process in the mind.

Conceptual Model - used to help us know and understand the subject matter they represent.

Conceptual Modeling is the **activity** of formally describing some aspects of the physical and social world around us for the purposes of understanding and communication.



Water flow in the plant-soil-atmosphere system



A colloid-facilitated solute transport

Mathematical Modeling

A **Mathematical Model** is a description of a physical system using mathematical concepts and language.

Flow and transport processes in the vadose zone are usually described using various **partial differential equations**.

Water flow, and solute and heat transport in the plant-soil-atmosphere system (HYDRUS-1D)

Variably-Saturated Water Flow (Richards Equation)

$$\frac{\partial \theta(h)}{\partial t} = \frac{\partial}{\partial z} \left[K(h) \left(\frac{\partial h}{\partial z} - 1 \right) \right] - S(h)$$

Solute Transport (Convection-Dispersion Equation)

$$\frac{\partial(\rho s)}{\partial t} + \frac{\partial(\theta c)}{\partial t} = \frac{\partial}{\partial z} \left(\theta D \frac{\partial c}{\partial z} - qc \right) - \phi$$

Heat Movement

$$\frac{\partial C_p(\theta)T}{\partial t} = \frac{\partial}{\partial z} \left[\lambda(\theta) \frac{\partial T}{\partial z} \right] - C_p \frac{\partial qT}{\partial z} - C_p ST$$

Colloid-Facilitated Solute Transport (C-Ride Module)

Mass Balance of Total Contaminant:

$$\frac{\partial \theta C}{\partial t} + \rho \frac{\partial S_i}{\partial t} + \rho \frac{\partial S_k}{\partial t} + \frac{\partial \theta_c C_s}{\partial t} + \rho \frac{\partial S_c}{\partial t} = \frac{\partial}{\partial x} \left(\theta D \frac{\partial C}{\partial x} - \theta q C \right) + \frac{\partial}{\partial x} \left(\theta_c S_m D_c \frac{\partial C_c}{\partial x} \right) - \frac{\partial q C_s}{\partial x} + R$$

Left hand side sums the Mass of Contaminant:

- in the liquid phase
 - sorbed instantaneously and kinetically to the solid phase
 - sorbed to mobile and immobile colloids
- Right hand side considers various Mass Fluxes
- dispersive and advective transport of the dissolved contaminant
 - dispersive and advective transport of contaminant sorbed to mobile colloids
 - and Transformation/Reaction (e.g., degradation).

Analytical Models

Analytical Models represent a classical mathematical approach to solve mathematical equations, leading to an exact solution for a particular problem.

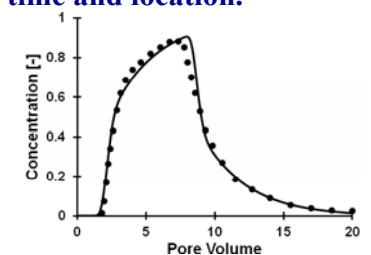
Analytical Models usually result in an explicit equation that states that concentration (or water content or temperature) is equal to a certain value at a particular time and location.

$$c(x,t) = \begin{cases} C_o B(x,t) + C_i A(x,t) + \frac{Z}{\mu} [1 - A(x,t) - B(x,t)] & 0 < t \leq t_o \\ C_o [B(x,t) - B(x,t-t_o)] + C_i A(x,t) + \frac{Z}{\mu} [(1 - A(x,t) - B(x,t))] & t > t_o \end{cases}$$

where

$$A(x,t) = \exp\left(-\frac{\mu t}{R}\right) \left\{ 1 - \frac{1}{2} \operatorname{erfc}\left[\frac{Rx-vt}{2\sqrt{DRt}}\right] - \sqrt{\frac{v^2 t}{\pi DR}} \exp\left[-\frac{(Rx-vt)^2}{4DRt}\right] + \frac{1}{2} \left(1 + \frac{vx}{D} + \frac{v^2 t}{DR} \right) \exp\left(\frac{vx}{D}\right) \operatorname{erfc}\left[\frac{Rx+vt}{2\sqrt{DRt}}\right] \right\}$$

$$B(x,t) = \frac{v}{u+v} \exp\left(\frac{(v-u)x}{2D}\right) \operatorname{erfc}\left[\frac{Rx-ut}{2\sqrt{DRt}}\right] - \frac{v}{u-v} \exp\left(\frac{(v+u)x}{2D}\right) \operatorname{erfc}\left[\frac{Rx+ut}{2\sqrt{DRt}}\right] + \frac{v^2}{2\mu D} \exp\left(\frac{vx}{D} - \frac{\mu t}{R}\right) \operatorname{erfc}\left[\frac{Rx+vt}{2\sqrt{DRt}}\right]$$

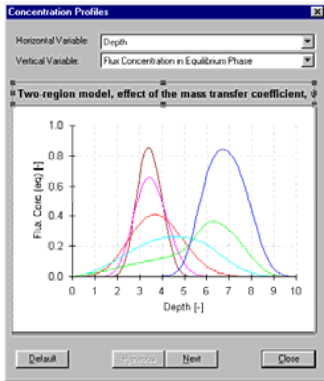


Observed (circles) and fitted (solid line) breakthrough curves for boron transport through a 30 cm long soil column filled with Glendale clay loam (van Genuchten, 1974).

STANMOD

Computer Software for Evaluating Solute Transport in Porous Media Using **Analytical Solutions** of the Convection-Dispersion Equation

J. Šimůnek, M. Th. van Genuchten, M. Šejna, N. Toride, and F. J. Leij



A powerful and very versatile Windows-based software package.

One-Dimensional Transport Models:

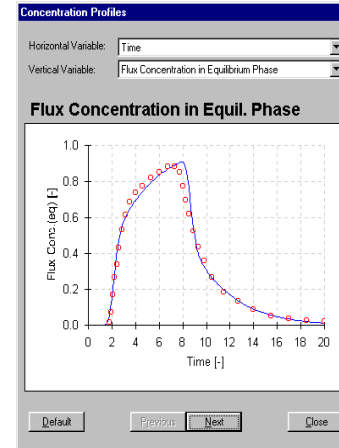
- CFITM** [van Genuchten, 1980]
- CFITM** [van Genuchten, 1981]
- CHAIN** [van Genuchten, 1985]
- CXTFIT2** [Toride et al., 1995]
- SCREEN** [Jury et al., 1987]

Two/Three-Dimensional Transport Models:

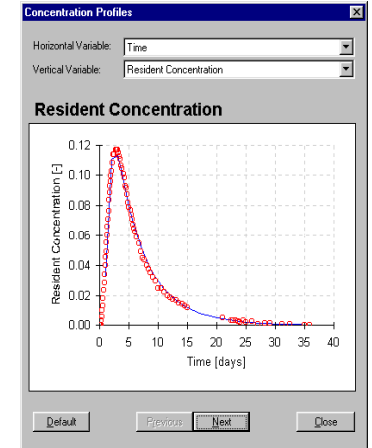
- 3DADE** [Leij and Bradford, 1994]
- N3DADE** [Leij and Toride, 1995]

STANMOD (1D Applications)

Inverse Analysis



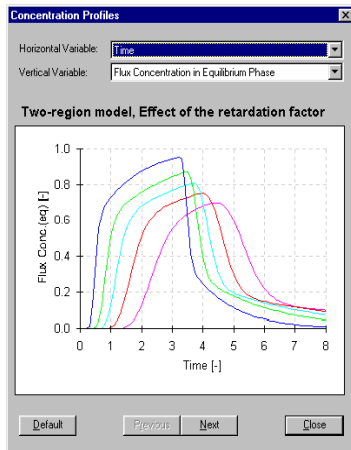
Deterministic Analysis



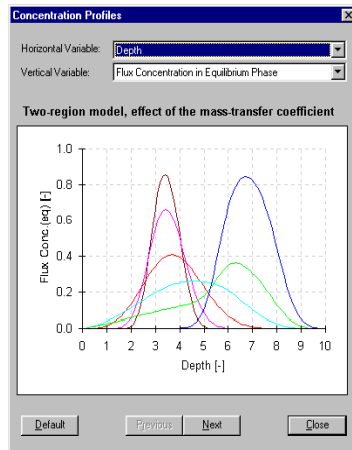
Stochastic Analysis

STANMOD (1D Applications)

Direct Analysis

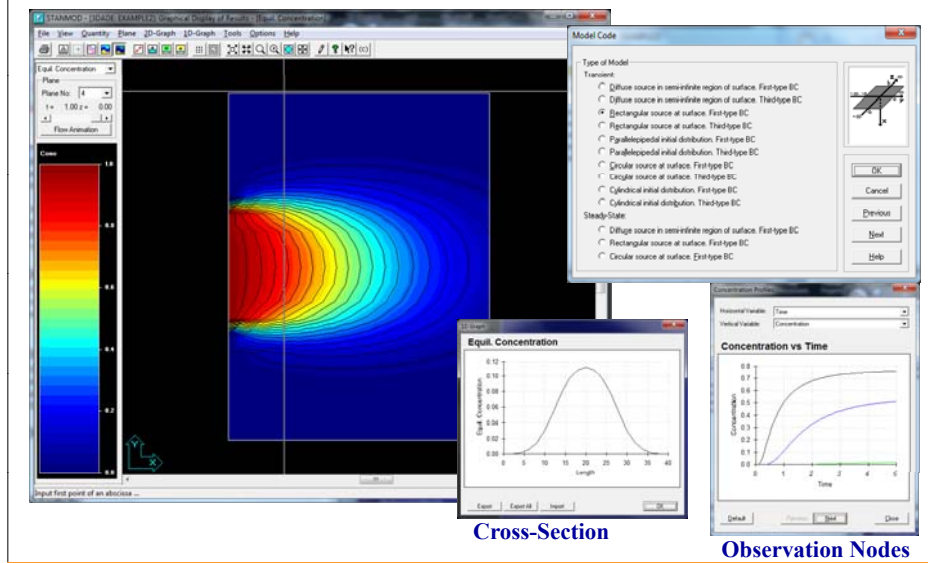


Retardation Factor



Mass Transfer Coefficient

STANMOD (2D Applications)



Cross-Section

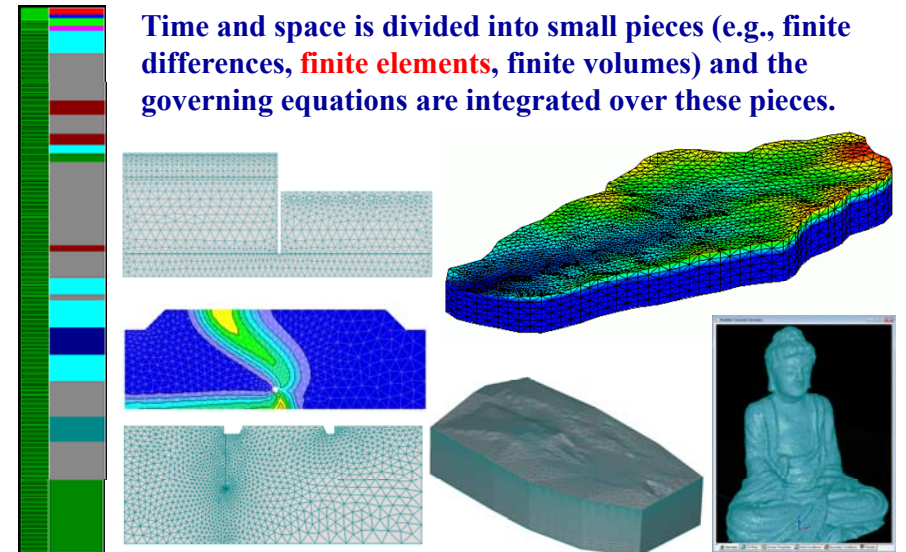
Observation Nodes

Analytical Models

- ◆ Using **Analytical Solutions** one can often more easily evaluate interrelationships among parameters and get better insight into how various processes control the basic flow and transport processes.
- ◆ **Analytical Solutions** are often used to check the correctness and accuracy of numerical models.
- ◆ Many **Analytical Solutions** lead to relatively complicated formulations that include infinite series and/or integrals.
- ◆ **Analytical Solutions** can usually be derived only for **simplified** transport systems involving linearized governing equations, homogeneous soils, simplified geometries of the transport domain, and constant or highly simplified initial and boundary conditions.
- ◆ For more **complex situations**, such as for transient water flow or nonequilibrium solute transport with nonlinear reactions, **Analytical Solutions** are generally not available and/or cannot be derived, in which case **Numerical Models** must be employed.

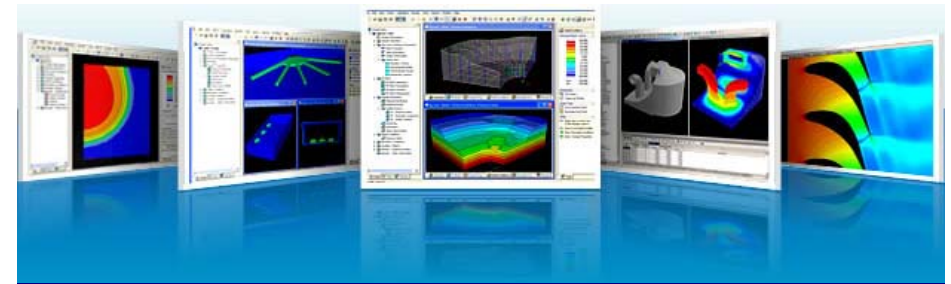
Numerical Modeling

Time and space is divided into small pieces (e.g., finite differences, **finite elements**, finite volumes) and the governing equations are integrated over these pieces.



Numerical Models

- ◆ **Numerical Methods** are superior to **Analytical Methods** in terms of being able to solve practical problems.
- ◆ **Numerical Methods** allow users
 - to design complicated geometries that reflect complex natural geologic and hydrologic conditions,
 - to control parameters in space and time,
 - to prescribe realistic initial and boundary conditions, and
 - to implement nonlinear constitutive relationships.
- ◆ **Numerical Methods** usually
 - subdivide the time and spatial coordinates into smaller pieces, such as finite differences, finite elements, or finite volumes, and
 - reformulate the continuous form of governing partial differential equations in terms of a system of algebraic eqs.
- ◆ In order to obtain solutions at certain times, **Numerical Methods** generally require intermediate simulations (time-stepping) between the initial condition and the points in time for which the solution is needed.

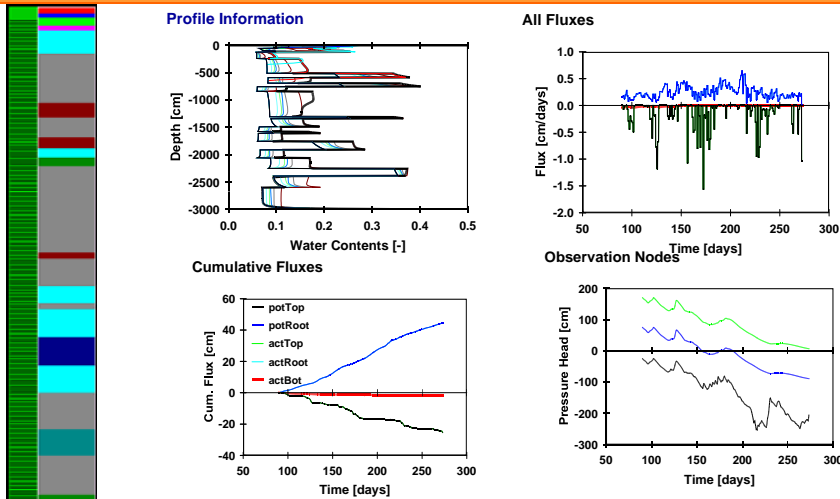


HYDRUS (1D/2D/3D)

Software for Simulating Water Flow and Solute Transport in **One/Two/Three** - Dimensional Variably-Saturated Soils Using **Numerical Solutions**

- thousands of users around the world
- thousands of applications published
- used by scientists, students, and/or practicing professionals

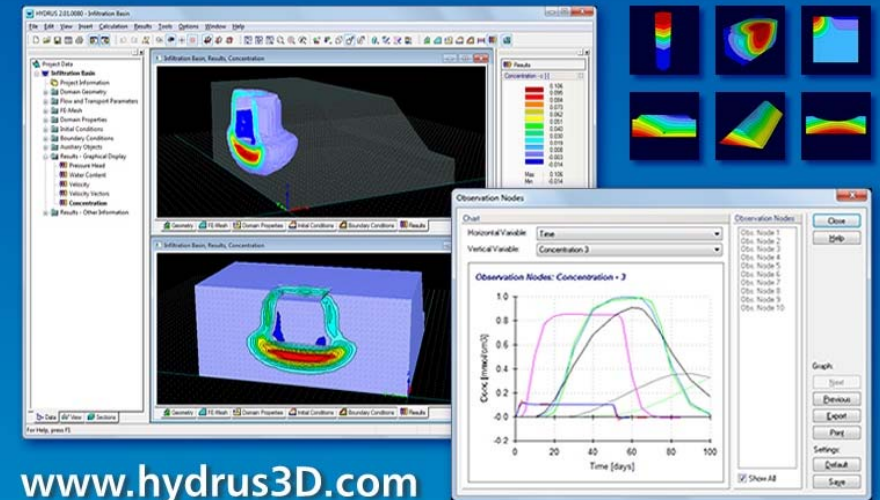
HYDRUS-1D



Software for Simulating Water Flow and Solute Transport in One-Dimensional Variably-Saturated Soils Using Numerical Solutions

HYDRUS

Software for simulating water, heat, and solute transport in variably saturated porous media.

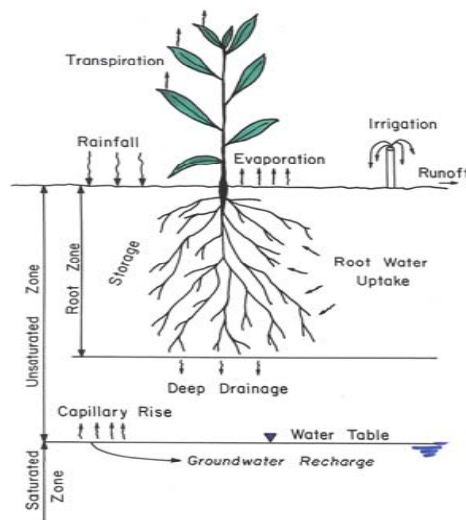


www.hydrus3D.com

Agricultural Applications

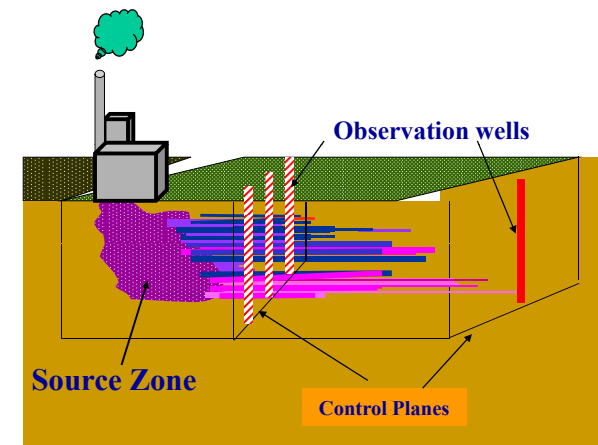
- ◆ Precipitation
- ◆ Irrigation
- ◆ Runoff
- ◆ Evaporation
- ◆ Transpiration
- ◆ Root Water Uptake
- ◆ Capillary Rise
- ◆ Deep Drainage

- ◆ Fertilizers
- ◆ Pesticides
- ◆ Fumigants
- ◆ Emerging Pollutants (steroids and hormones, pharmaceuticals)
- ◆ Colloids
- ◆ Pathogens
- ◆ Nanoparticles



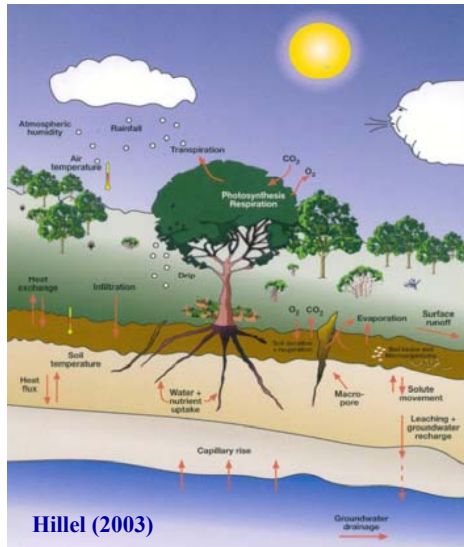
Industrial Applications

- ◆ Industrial Pollution
- ◆ Municipal Pollution
- ◆ Landfill Covers
- ◆ Waste Repositories
- ◆ Radioactive Waste Disposal Sites
- ◆ Remediation
- ◆ Brine Releases
- ◆ Contaminant Plumes
- ◆ Seepage of Wastewater from Land Treatment Systems
- ◆ Emerging Pollutants (gasoline additives, industrial additives, personal hygiene products, flame retardants, explosives, surfactants)



Environmental Applications

- ◆ Ecological Apps
- ◆ Heat Exchange and Fluxes (including the **Surface Energy Balance**)
- ◆ **Carbon** Storage and Fluxes
- ◆ Nutrient Transport
- ◆ Soil Respiration
- ◆ Microbiological Processes
- ◆ Effects of Climate Change
- ◆ Riparian Systems
- ◆ Stream-Aquifer Interactions



Governing Equations

Variably-Saturated Water Flow (**Richards Equation**)

$$\frac{\partial \theta(h)}{\partial t} = \frac{\partial}{\partial z} \left[K(h) \left(\frac{\partial h}{\partial z} - 1 \right) \right] - S(h)$$

Solute Transport (**Convection-Dispersion Equation**)

$$\frac{\partial(\rho s)}{\partial t} + \frac{\partial(\theta c)}{\partial t} = \frac{\partial}{\partial z} \left(\theta D \frac{\partial c}{\partial z} \right) - \frac{\partial qc}{\partial z} - \phi$$

Heat Movement (**Conduction-Dispersion Equation**)

$$\frac{\partial C_p(\theta)T}{\partial t} = \frac{\partial}{\partial z} \left[\lambda(\theta) \frac{\partial T}{\partial z} \right] - C_w \frac{\partial qT}{\partial z} - C_w ST$$

HYDRUS – Main Processes

Water Flow:

- ◆ Richards equation for variably-saturated water flow
- ◆ Various models of soil hydraulic properties
- ◆ Hysteresis
- ◆ Sink term, accounting for water uptake by plant roots (uncompensated and compensated; reduced due to osmotic and pressure stress)
- ◆ Preferential flow
- ◆ Isothermal and thermal liquid and vapor flow

Solute Transport:

- ◆ Convective-dispersive transport in the liquid phase
- ◆ Diffusion in the gaseous phase
- ◆ Linear and nonlinear interactions between the solid and liquid phases
- ◆ Linear equilibrium reactions between the liquid and gaseous phases
- ◆ Zero-order production, First-order degradation
- ◆ Physical and chemical nonequilibrium solute transport
- ◆ Sink term, accounting for nutrient uptake by plant roots (active and passive)

Heat Transport:

- ◆ Conduction and convection with flowing water (transport of latent heat)

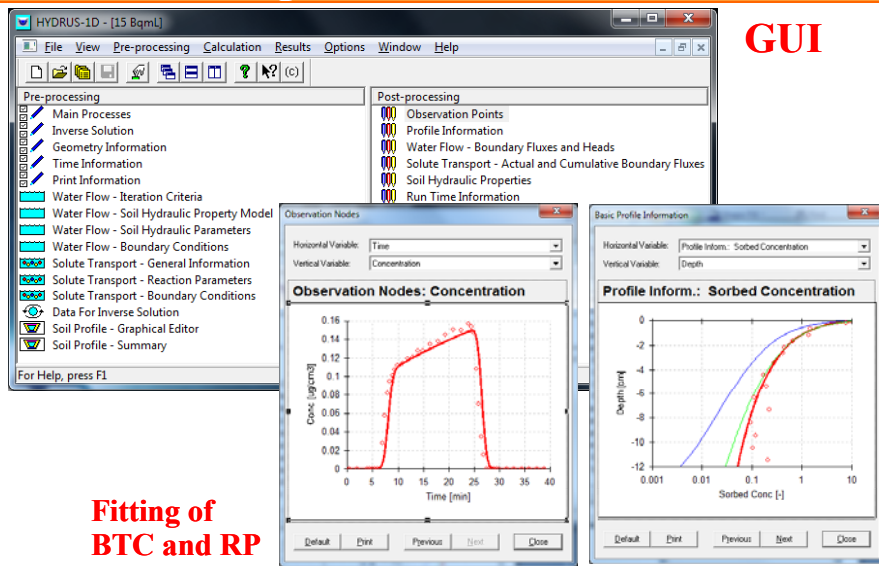
Inverse Optimization (of flow, transport, and reaction parameters)

HYDRUS – Solute Transport

- ◆ Transport of **Single Ions or Particles** (colloids, viruses, bacteria)
- ◆ Transport of **Multiple Ions** (sequential first-order decay)
 - ◆ Radionuclides: $^{238}\text{Pu} \rightarrow ^{234}\text{U} \rightarrow ^{230}\text{Th} \rightarrow ^{226}\text{Ra}$
 - ◆ Nitrogen: $(\text{NH}_2)_2\text{CO} \rightarrow \text{NH}_4^+ \rightarrow \text{NO}_2^- \rightarrow \text{NO}_3^-$
 - ◆ Pesticides: aldicarb (oxime) \rightarrow sulfone (sulfone oxime) \rightarrow sulfoxide (sulfoxide oxime)
 - ◆ Chlorinated Hydrocarbons: PCE \rightarrow TCE \rightarrow c-DCE \rightarrow VC \rightarrow ethylene
 - ◆ Pharmaceuticals, Hormones: Estrogen (17 β Estradiol \rightarrow Estrone \rightarrow Estriol), Testosterone
 - ◆ Explosives: TNT (\rightarrow 4HADNT \rightarrow 4ADNT \rightarrow TAT), RDX, HMX
- ◆ Transport of Major Ions (the **UNSATCHEM** module)
- ◆ General **BioGeoChemical** Reactions (the **HP1/2/3** module)
- ◆ Processes in Wetlands (the **CW2D** and **CWM1** modules)
- ◆ Colloid-Facilitated Solute Transport (the **C-Ride** module)

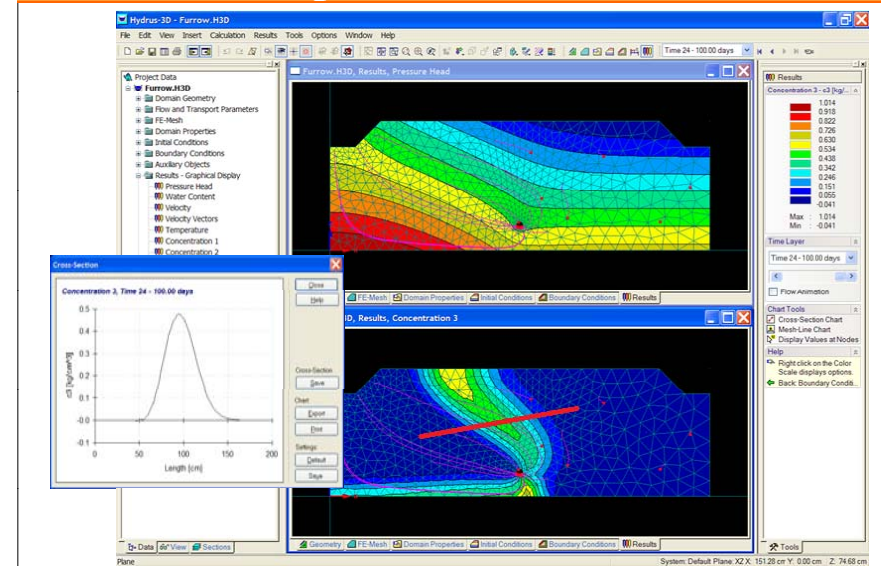
HYDRUS-1D Graphical User Interface

GUI

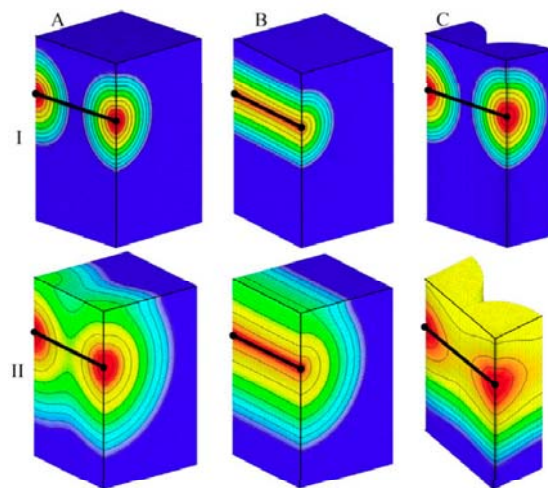


Fitting of
BTC and RP

HYDRUS (2D/3D) Graphical User Interface



HYDRUS (2D/3D) - Applications



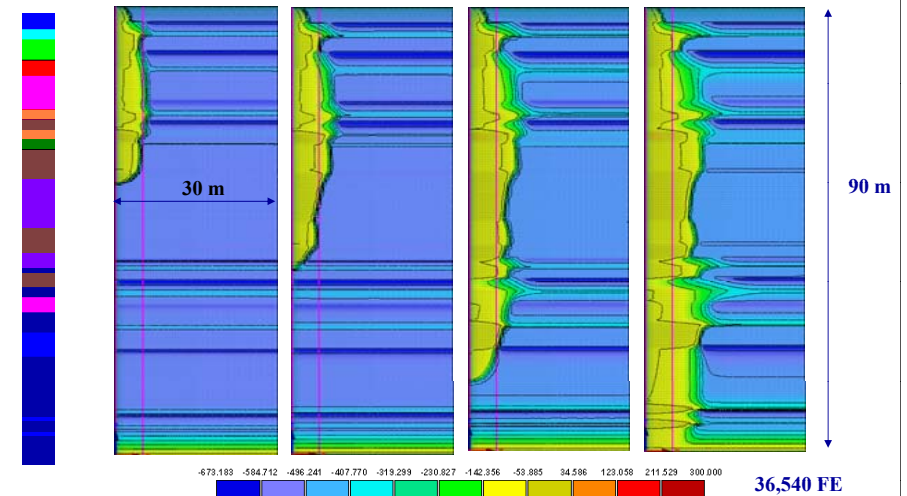
Subsurface Drip Irrigation System

Soil water content
simulated as:

- A. a **Three-Dimensional** system with **multiple point sources**
- B. a **Two-Dimensional** system with a **line source**
- C. An **Axisymmetrical** two-dimensional system with a **point source**

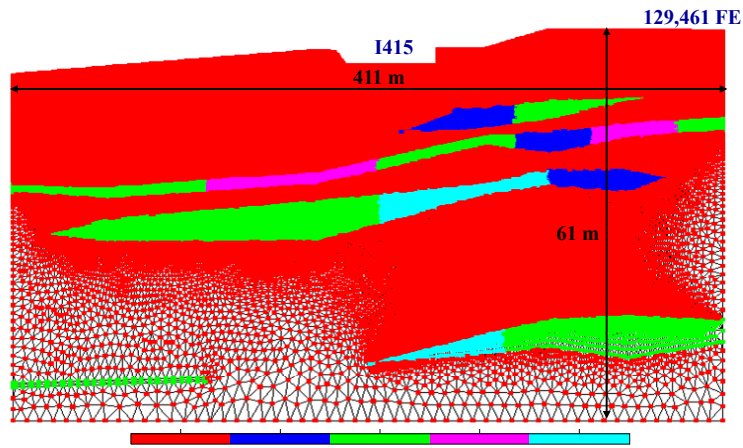
Kandelous, M. M., J. Šimůnek, M. Th. van Genuchten, and K. Malek, Soil water content distributions between two emitters of a subsurface drip irrigation system, *Soil Science Society of America Journal*, 75(2), 488-497, 2011.

HYDRUS (2D/3D) - Applications



Pressure head profiles after 10, 25, 50, and 100 years.
Leak (2 mm diameter) at the bottom of the Palmdale Reservoir.

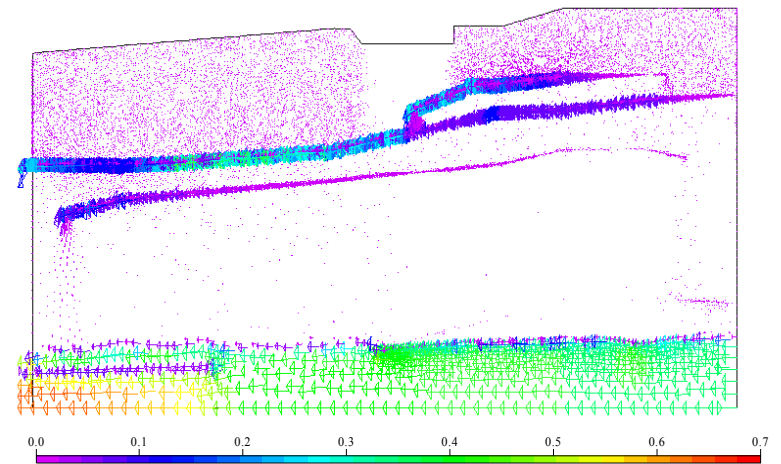
HYDRUS (2D/3D) - Applications



Finite Element Mesh and Material Distribution

A two-dimensional transect, 411 m wide and 61 m deep, with a freeway in the middle

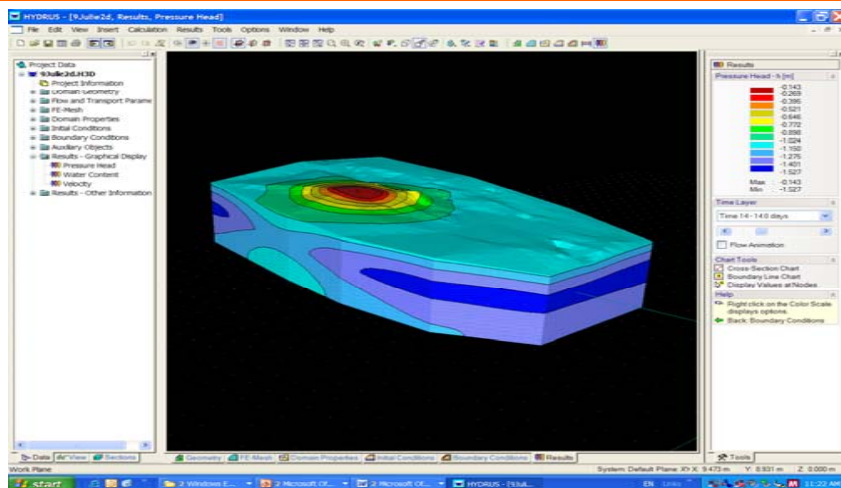
HYDRUS (2D/3D) - Applications



Velocity Vectors

A two-dimensional transect, 411 m wide and 61 m deep, with a freeway in the middle

HYDRUS (2D/3D) - Applications



Pressure Head Distribution
in a Three-Dimensional Transport Domain

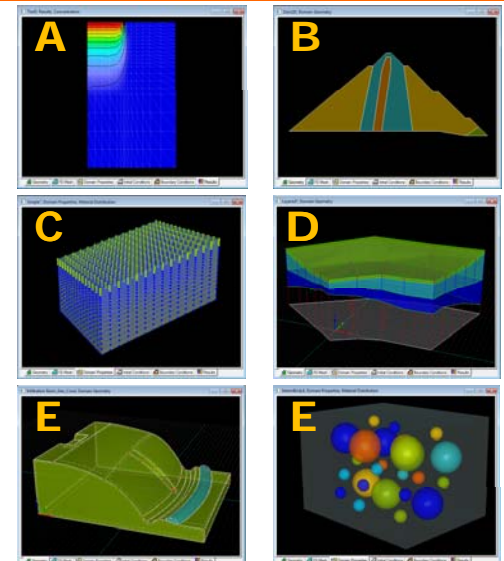
HYDRUS (2D/3D) – Transport Domains

HYDRUS Geometries:

- A. 2D – Simple
- B. 2D – General
- C. 3D – Simple
- D. 3D – Layered
- E. 3D – General

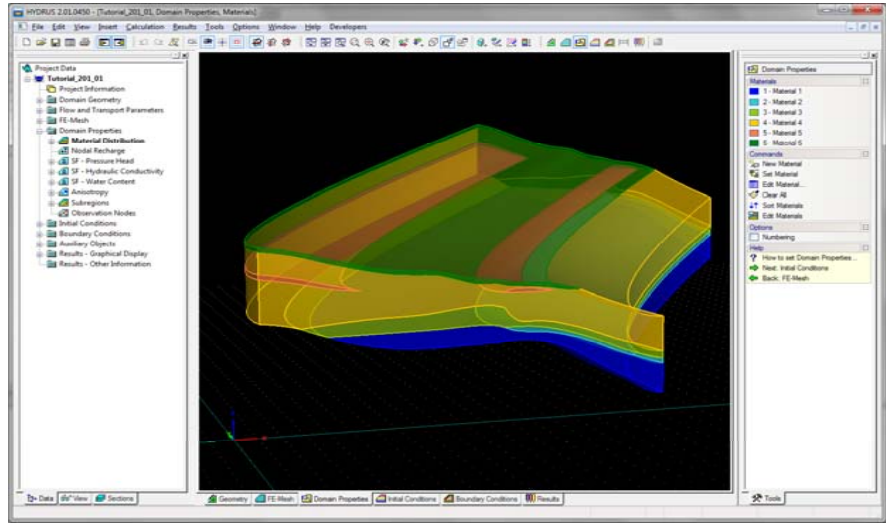
HYDRUS Levels:

- 2D – Lite (A)
- 2D – Standard (A+B)
- 3D – Lite (A+C)
- 3D – Standard (A+B+C+D)
- 3D – Professional (All)



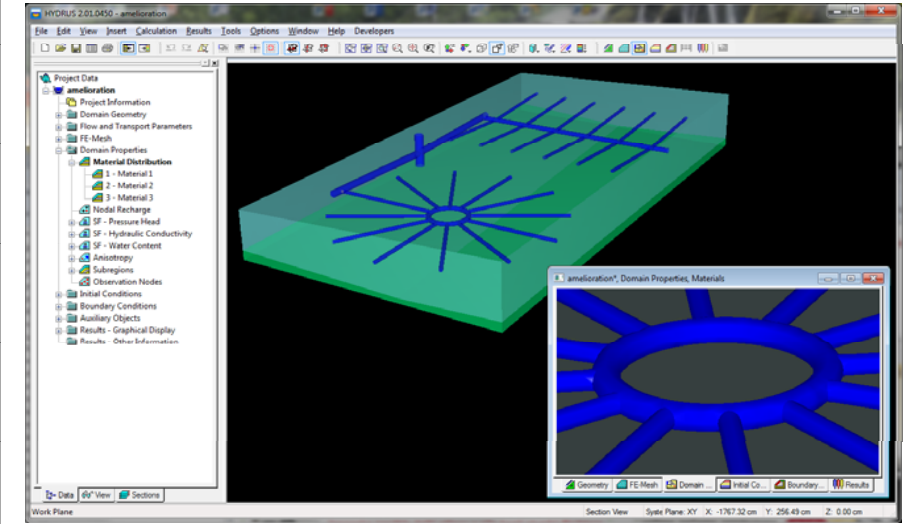
HYDRUS (2D/3D) - Geometries

Discontinuous 3D Layers



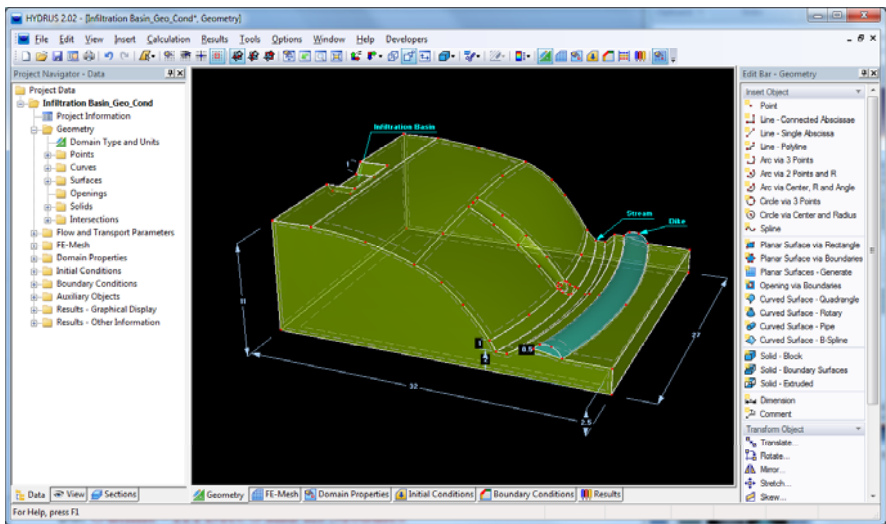
HYDRUS (2D/3D) - Geometries

Complex Drainage System



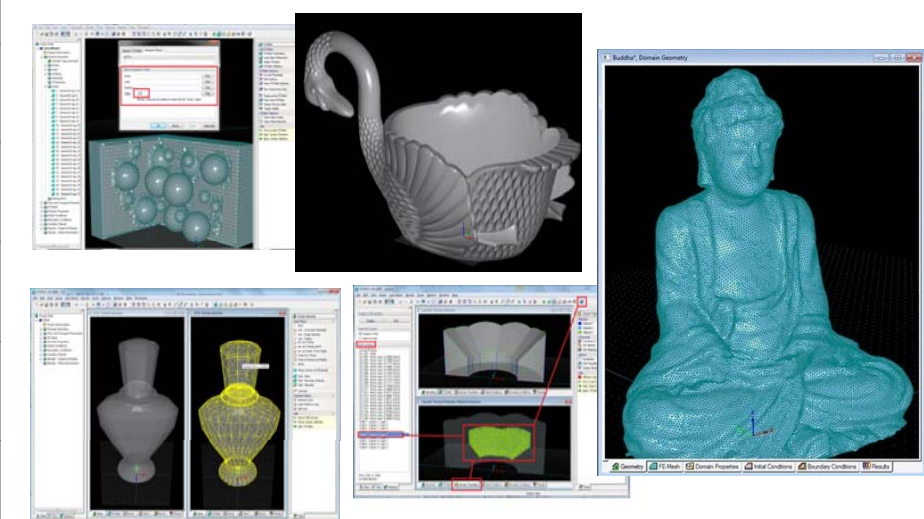
HYDRUS: 3D-Professional

Infiltration Basin and Stream



HYDRUS (2D/3D) - Geometries

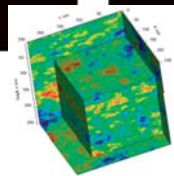
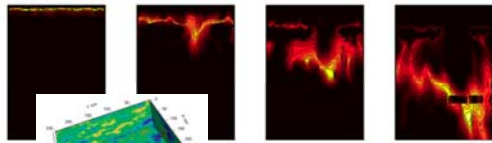
Import of complex Geometries (e.g., DXF, TIN, STL)



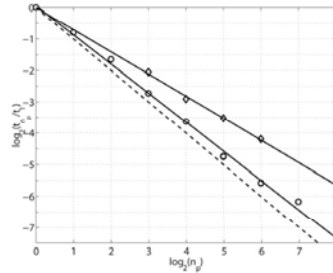
ParSWMS – Parallelized Version of HYDRUS

- ◆ **ParSWMS** (Hardelauf et al., 2007) - Parallelized version of **SWMS_3D**, an earlier and simpler version of **HYDRUS-3D**.
- ◆ Developed by the *Forschungszentrum in Jülich, Germany*.
- ◆ **MPI** (Message-Passing Interface). LINUX or UNIX OSs.
- ◆ **Test** - Supercomputer with 41 SMP nodes with 32 processors each (total 1312 processors)

2D Water flow and solute transport (Hardelauf et al., 2007)
492,264 finite element nodes



3D Water flow problem
275,706 finite element nodes
(Herbst et al., 2008)



HYDRUS and its Modules

- ◆ **HYDRUS + PHREEQC = HP1/2/3**
(hydrological + biogeochemical processes)
- ◆ **HYDRUS + C-Ride**
(particle and particle-facilitated solute transport)
- ◆ **HYDRUS + DualPerm**
(preferential water flow and solute transport)
- ◆ **HYDRUS + UNSATCHEM**
(hydrological + CO₂ + major ion processes)
- ◆ **HYDRUS + Wetland (CW2D/CWM1)**
(biogeochemical processes in constructed wetlands)
- ◆ **HYDRUS + Fumigant**
(fate and transport of fumigants)

HYDRUS and its Modules

- ◆ **HYDRUS + PHREEQC = HP1/2/3**
(hydrological + biogeochemical processes)
- ◆ **HYDRUS + C-Ride**
(particle and particle-facilitated solute transport)
- ◆ **HYDRUS + DualPerm**
(preferential water flow and solute transport)
- ◆ **HYDRUS + UNSATCHEM**
(hydrological + CO₂ + major ion processes)
- ◆ **HYDRUS + Wetland (CW2D/CWM1)**
(biogeochemical processes in constructed wetlands)
- ◆ **HYDRUS + Fumigant**
(fate and transport of fumigants)

HP1/2/3 (HYDRUS+PHREEQC)

Simulating water flow, transport and biogeochemical reactions in environmental soil quality problems

HPx

A Coupled Numerical Code for
Variably Saturated Water Flow,
Solute Transport and
BioGeoChemistry
in Soil Systems

HP1/2/3

Flow and transport model
HYDRUS-1D 4.0
HYDRUS (2D/3D) 2.x

Biogeochemical model
PHREEQC-2.4

HP1/2/3 (HYDRUS+PHREEQC)

HYDRUS-1D or HYDRUS (2D/3D):

- ◆ Variably-Saturated Water Flow
- ◆ Solute Transport
- ◆ Heat Transport
- ◆ Gas Transport
- ◆ Root Water Uptake

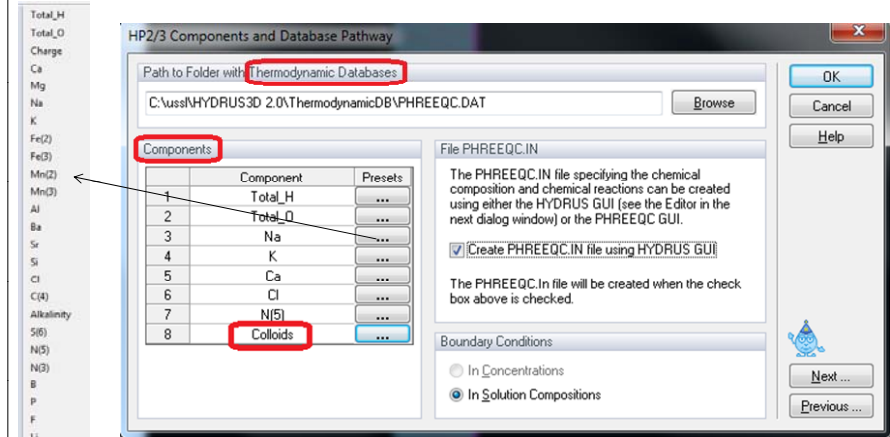


PHREEQC [Parkhurst and Appelo, 1999]:

Available Chemical Reactions:

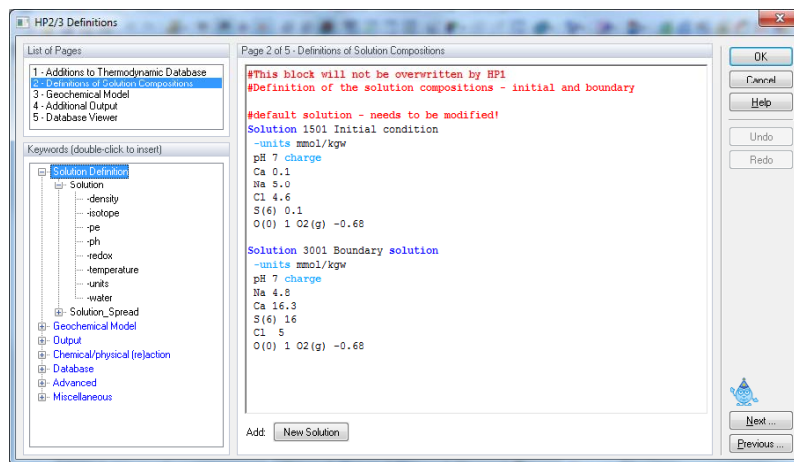
- ◆ Aqueous Complexation
- ◆ Redox Reactions
- ◆ Ion Exchange (Gains-Thomas)
- ◆ Surface Complexation (diffuse double-layer model and non-electrostatic surface complexation model)
- ◆ Precipitation/Dissolution
- ◆ Chemical Kinetics
- ◆ Biological Reactions

HYDRUS GUI for HP1/2/3



Jacques, D., and J. Šimunek, Notes on the HP1 software – a coupled code for variably-saturated water flow, heat transport, solute transport and biogeochemistry in porous media, HP1 Version 2.2, SCK•CEN-BLG-1068, Waste and Disposal, SCK•CEN, Mol, Belgium, 114 pp., 2010.

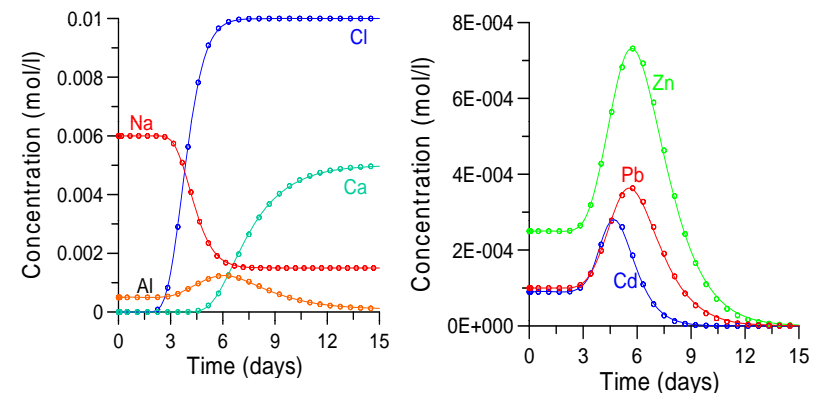
HYDRUS (2D/3D) GUI for HP2/3



Four text editors to define the geochemical model, required output, and solution compositions are fully incorporated into the GUI.

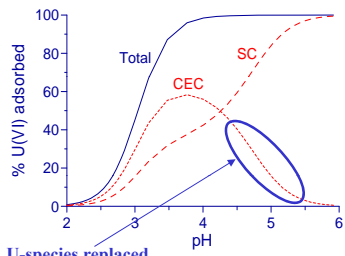
Transport and Cation Exchange Heavy Metals

Major ions (Ca, Na, Al, Cl) and Heavy Metals (Zn, Pb, Cd)



A (8-cm) soil column is initially contaminated with heavy metals (in equilibrium with the cation exchanger). The column is then flushed with a CaCl₂ solution without heavy metals.

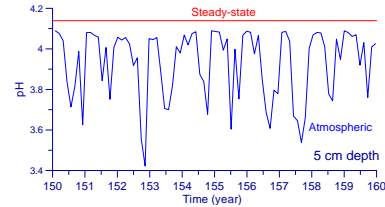
U-Transport in Agricultural Field Soils



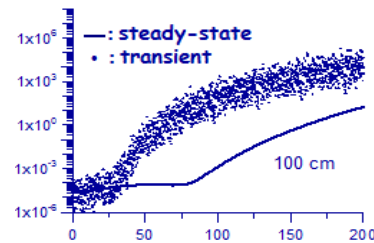
U-species replaced by other cations → Increased deprotonation → Increased U-sorption

- ◆ **Aqueous speciation reactions**
C, Ca, Cl, F, H, K, Mg, N(5), Na, O(0), O(-2), P, S(6), U(6)
- ◆ **Multi-site cation exchange reactions**
 - Related to amount of organic matter
 - Increases with increasing pH
 - UO_2^{2+} adsorbs
- ◆ **Surface complexation reactions**
 - Specific binding to charged surfaces (=FeOH)
 - Related to amount of Fe-oxides

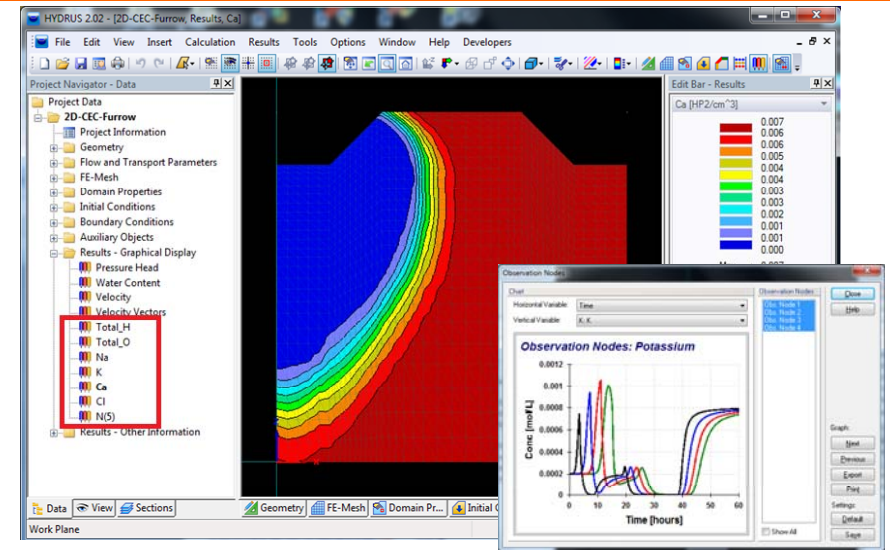
Jacques et al., VZJ, 2008.



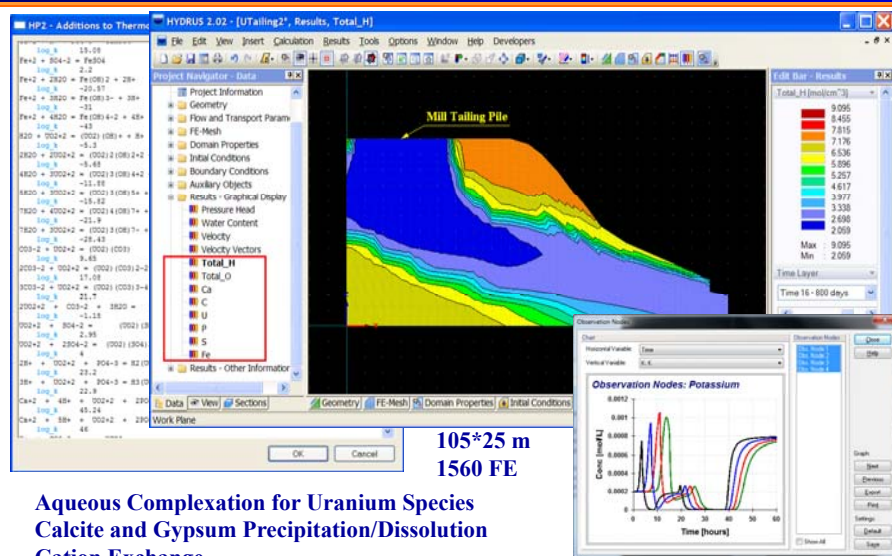
- ◆ Water content variations induce pH variations (dry soil => low pH)
- ◆ pH variations => variations in sorption potential (low pH => low sorption – higher mobility)



HP2 – Reclamation of a Sodic Soil



Uranium Transport from a Mill Tailing Pile



HP1 Examples

- ◆ Transport of **Heavy Metals** (Zn^{2+} , Pb^{2+} , and Cd^{2+}) subject to a multiple **pH-dependent Cation Exchange**
- ◆ Transport and mineral dissolution of **Amorphous SiO_2** and **Gibbsite**
- ◆ Infiltration of a **Hyperalkaline Solution** in a clay sample (kinetic precipitation-dissolution of kaolinite, illite, quartz, calcite, dolomite, gypsum, hydrocalcite, and sepiolite)
- ◆ Kinetic biodegradation of **NTA** (biomass, cobalt)
- ◆ Long-term **Uranium** transport following mineral phosphorus fertilization (pH-dependent surface complexation and cation exchange)
- ◆ Transport of **Explosives**, such as TNT and RDX
- ◆ **Property Changes** (porosity/conductivity) due to precipitation/ dissolution reactions

HYDRUS and its Modules

- ◆ HYDRUS + PHREEQC = HP1/2/3
(hydrological + biogeochemical processes)
- ◆ HYDRUS + C-Ride
(particle and particle-facilitated solute transport)
- ◆ HYDRUS + DualPerm
(preferential water flow and solute transport)
- ◆ HYDRUS + UNSATCHEM
(hydrological + CO₂ + geochemical processes)
- ◆ HYDRUS + Wetland (CW2D/CWM1)
(biogeochemical processes in constructed wetlands)
- ◆ HYDRUS + Fumigant
(fate and transport of fumigants)

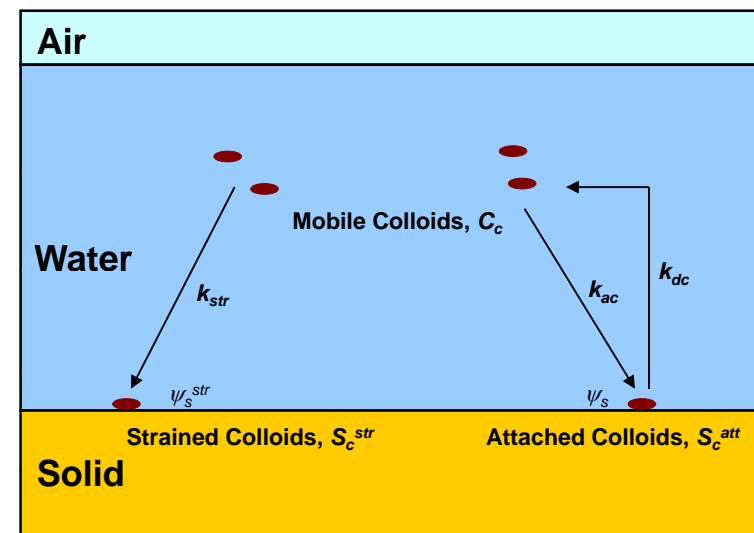
Colloid-Facilitated Solute Transport

- ◆ Many **contaminants** should be relatively immobile in the subsurface since under normal conditions they are **strongly sorbed to soil**
- ◆ They can also sorb to colloids, which often move at rates similar or faster as non-sorbing tracers
- ◆ Experimental evidence exists that many contaminants are transported not only in a dissolved state by water, but also sorbed to **moving colloids**
- ◆ Examples: **heavy metals**, **radionuclides**, **pesticides**, **viruses**, **pharmaceuticals**, **hormones**, and other contaminants

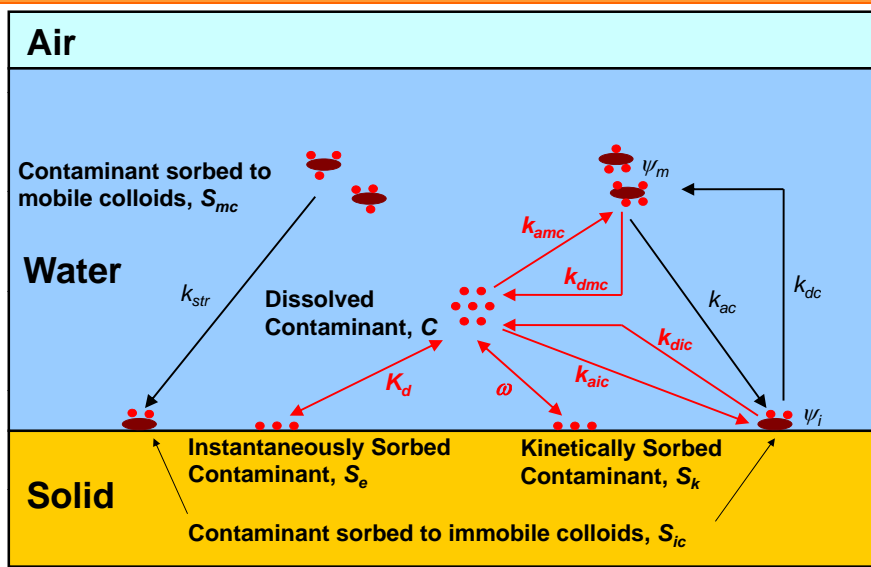
HYDRUS + C-Ride Module

- ◆ **HYDRUS-1D and HYDRUS (2D/3D)**
 - Variably-Saturated Water Flow
 - Solute Transport
 - Heat Transport
 - Root Water Uptake
- ◆ **C-Ride** (Šimůnek et al., 2006)
 - **Particle Transport**
 - colloids, bacteria, viruses, nanoparticles
 - attachment/detachment, straining, blocking
 - **Particle-Facilitated Solute Transport**
 - transport of solutes attached to particles

Colloid, Virus, and Bacteria Transport

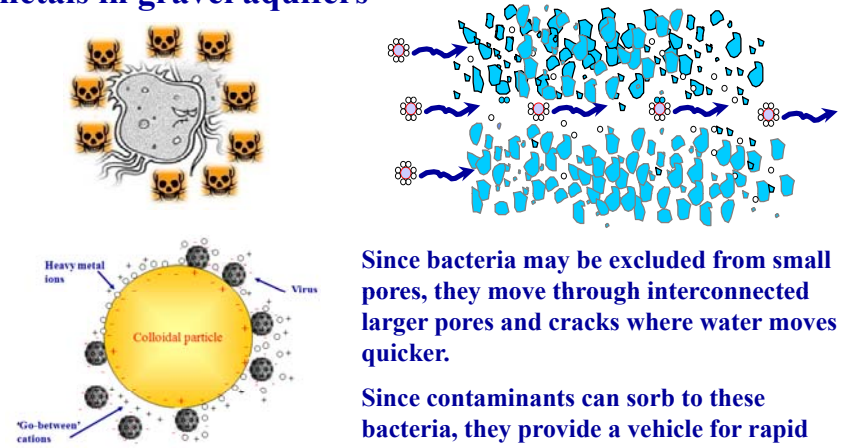


Colloid-Facilitated Solute Transport

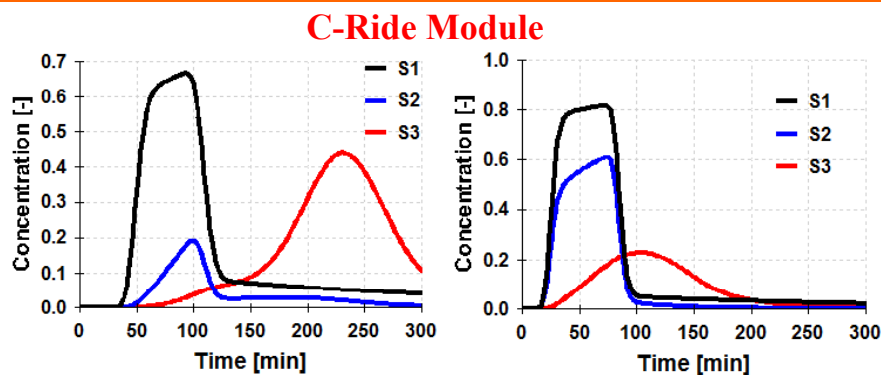


Particle-Facilitated Solute Transport

Pang et al. [2005]: Bacteria act as carriers for heavy metals in gravel aquifers



Colloid-Facilitated Solute Transport



Breakthrough curves for colloids (black line), solute sorbed to colloids (blue line), and dissolved solute (red line):

Left: solute and colloids are applied independently

Right: solute is initially attached to colloids

The Retardation Factor for colloids is equal to 1 and for solute to 4
Unit input concentrations.

HYDRUS and its Modules

- ◆ HYDRUS + PHREEQC = HP1/2/3 (hydrological + biogeochemical processes)
- ◆ HYDRUS + C-Ride (particle and particle-facilitated solute transport)
- ◆ **HYDRUS + DualPerm** (preferential water flow and solute transport)
- ◆ HYDRUS + UNSATCHEM (hydrological + CO₂ + geochemical processes)
- ◆ HYDRUS + Wetland (CW2D/CWM1) (biogeochemical processes in constructed wetlands)
- ◆ HYDRUS + Fumigant (fate and transport of fumigants)

Preferential Flow and Transport

Fractured Rock



Macroporous Soil



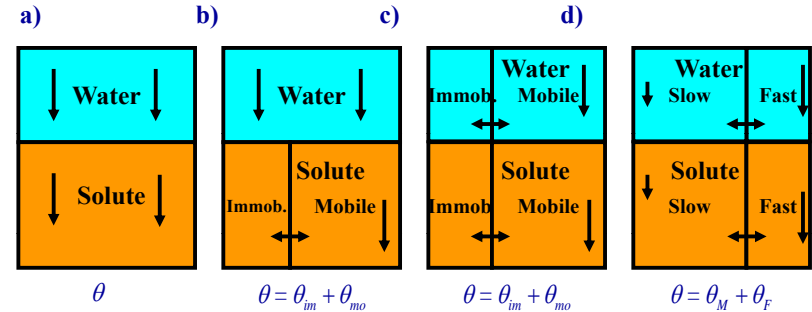
Heterogeneous Sediments



The DualPerm Module

Physical Nonequilibrium Solute Transport Models

Šimůnek and van Genuchten (2008):



a) Uniform Flow

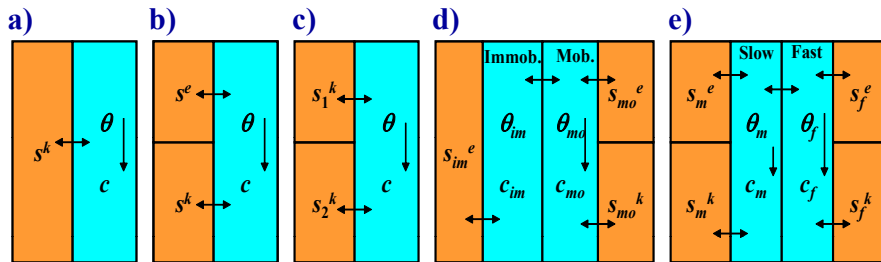
b) Mobile-Immobile Water

c) Dual-Porosity (Šimůnek et al., 2003)

d) Dual-Permeability (Gerke and van Genuchten, 1993)

Chemical Nonequilibrium Solute Transport Models

Šimůnek and van Genuchten (2008):



a) One-Site Kinetic Model

b) Two-Site Model (kinetic and instantaneous sorption)

c) Two Kinetic Sites Model

(particle transport, e.g., colloids, viruses, bacteria)

d) Dual-Porosity with One Kinetic Site Model

e) Dual-permeability with Two-Site Model

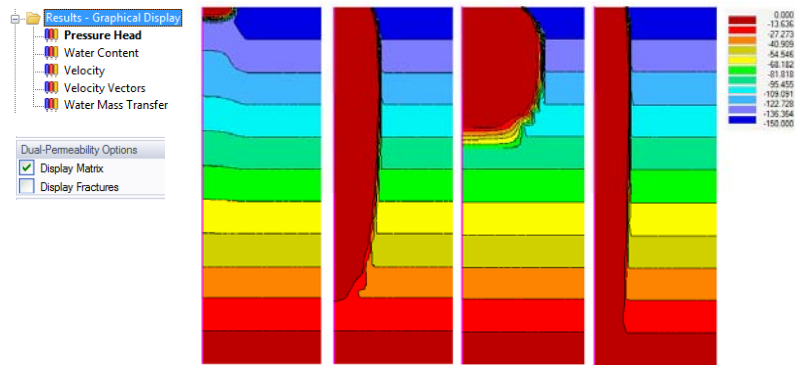
Nonequilibrium Models in the HYDRUS GUI

Variably-Saturated Water Flow

Solute Transport

The DualPerm Module – An Application

Water flow and Solute Transport in Dual-Permeability Variably-Saturated Porous Media



Pressure head profiles for the matrix (left), isotropic fracture, and fracture with $K_x^A/K_z^A=10$, and fracture with $K_x^A/K_z^A=0.1$ (right).

HYDRUS and its Modules

- ◆ HYDRUS + PHREEQC = HP1/2/3 (hydrological + biogeochemical processes)
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- ◆ HYDRUS + Fumigant (fate and transport of fumigants)

HYDRUS + UNSATCHEM

- ◆ **HYDRUS-1D and HYDRUS (2D/3D)**
 - Variably-Saturated Water Flow
 - Solute Transport
 - Heat Transport
 - Root Water Uptake
- ◆ **UNSATCHEM** (Šimůnek et al., 1996)
 - Carbon Dioxide Transport and Production
 - Major Ion Chemistry
 - Cation Exchange
 - Precipitation-Dissolution (instantaneous and kinetic)
 - Aqueous Complexation

UNSATCHEM Module

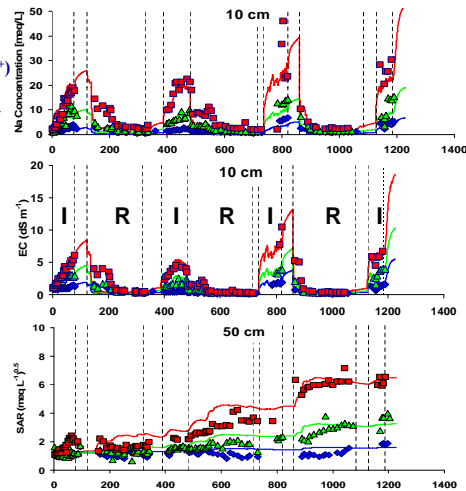
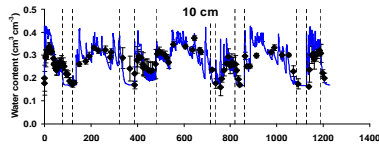
1	Aqueous Components	7	Ca ²⁺ , Mg ²⁺ , Na ⁺ , K ⁺ , SO ₄ ²⁻ , Cl ⁻ , NO ₃ ⁻
2	Complexed Species	10	CaCO ₃ ⁰ , CaHCO ₃ ⁺ , CaSO ₄ ⁰ , MgCO ₃ ⁰ , MgHCO ₃ ⁺ , MgSO ₄ ⁰ , NaCO ₃ ⁻ , NaHCO ₃ ⁰ , NaSO ₄ ⁻ , KSO ₄ ⁻
3	Precipitated Species	6	CaCO ₃ , CaSO ₄ ·2H ₂ O, CaMg(CO ₃) ₂ , MgCO ₃ ·3H ₂ O, Mg ₅ (CO ₃) ₄ (OH) ₂ ·4H ₂ O, Mg ₂ Si ₃ O _{7,5} (OH)·3H ₂ O
4	Sorbed Species (exchangeable)	4	XCa, XMg, XNa, XK
5	CO ₂ -H ₂ O Species	7	P _{CO2} , H ₂ CO ₃ [*] , CO ₃ ²⁻ , HCO ₃ ⁻ , H ⁺ , OH ⁻ , H ₂ O
6	Silica Species	3	H ₄ SiO ₄ , H ₃ SiO ₄ ⁻ , H ₂ SiO ₄ ²⁻

Kinetic reactions: calcite precipitation/dissolution, dolomite dissolution
Activity coefficients: extended Debye-Hückel equations, Pitzer expressions

UNSATCHEM - Lysimeter Study

To evaluate the effectiveness of HYDRUS to predict:

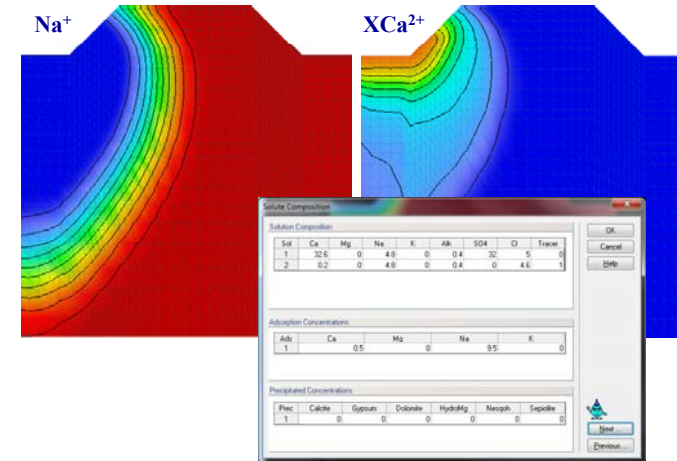
- ◆ Water content and fluxes
- ◆ Concentration of individual cations (e.g., Ca^{2+} , Mg^{2+})
- ◆ Overall salinity (Electrical conductivity – EC)
- ◆ Sodium Adsorption Ratio (SAR)
- ◆ Exchangeable Sodium Percentage (ESP)



Gonçalves, M. C., J. Šimůnek, T. B. Ramos, J. C. Martins, M. J. Neves, and F. P. Pires, Multicomponent solute transport in soil lysimeters irrigated with waters of different quality, *Water Resources Research*, 42, 17 pp., 2006.
 Ramos, T. B., J. Šimůnek, M. C. Gonçalves, J. C. Martins, A. Prazeres, N. L. Castanheira, and L. S. Pereira, Field evaluation of a multicomponent solute transport model in soils irrigated with saline waters, *J. of Hydrology*, 407(1-4), 129-144, 2011.

UNSATCHEM-2D Module

Major Ion Chemistry Module



- Results - Graphical Display
- Pressure Head
 - Water Content
 - Velocity
 - Velocity Vectors
 - Calcium
 - Magnesium
 - Sodium
 - Potassium
 - Alkalinity
 - Sulfate
 - Chloride
 - Tracer
 - Sorbed Calcium
 - Sorbed Magnesium
 - Sorbed Sodium
 - Sorbed Potassium
 - Calcite
 - Gypsum
 - Dolomite
 - Nesquehonite
 - Hydromagnesite
 - Sepiolite

Šimůnek, J., and D. L. Suarez, Two-dimensional transport model for variably saturated porous media with major ion chemistry, *Water Resources Research*, 30(4), 1115-1133, 1994.

HYDRUS and its Modules

- ◆ HYDRUS + PHREEQC = HP1/2/3 (hydrological + biogeochemical processes)
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- ◆ HYDRUS + DualPerm (preferential water flow and solute transport)
- ◆ HYDRUS + UNSATCHEM (hydrological + CO₂ + geochemical processes)
- ◆ **HYDRUS + Wetland (CW2D/CWM1)** (biogeochemical processes in constructed wetlands)
- ◆ HYDRUS + Fumigant (fate and transport of fumigants)

Wetland Module

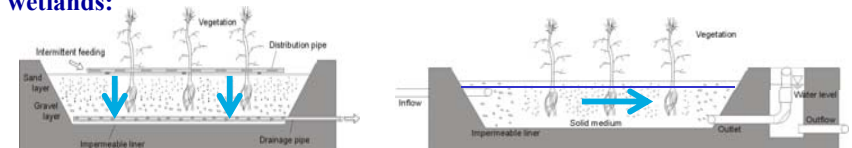
Constructed Wetlands (CWs) or wetland treatment systems

- ◆ are systems designed to **improve water quality**
- ◆ use the same processes that occur in natural wetlands but have the flexibility of being constructed
- ◆ effective in treating organic matter, nitrogen, phosphorus, and additionally for decreasing the concentrations of heavy metals, organic chemicals, and pathogens

CW2D : aerobic and anoxic processes for organic matter, nitrogen and phosphorus (Langergraber and Šimůnek, 2005)

CWM1: aerobic, anoxic and anaerobic processes for organic matter, nitrogen and sulphur (Langergraber et al., 2005)

Subsurface **Vertical (CW2D)** and **Horizontal (CWM1)** flow constructed wetlands:



Wetland Modules: Components

CW2D : aerobic and anoxic processes for organic matter, nitrogen and phosphorus
CWM1: aerobic, anoxic and anaerobic processes for organic matter, nitrogen and sulphur
Components:

CW2D (Langergraber and Šimůnek, 2005)	CWM1 (Langergraber et al., 2009b)
Organic matter, nitrogen, phosphorus	Organic matter, nitrogen, sulphur
CW2D components	Soluble components:
1. SO: Dissolved oxygen, O ₂ .	1. SO: Dissolved oxygen, O ₂ .
2. CR: Readily biodegradable soluble COD.	2. SF: Fermentable, readily biodegradable soluble COD.
3. CS: Slowly biodegradable soluble COD.	3. SA: Fermentation products as acetate.
4. CI: Inert soluble COD.	4. SI: Inert soluble COD.
5. XH: Heterotrophic bacteria	5. SNH: Ammonium and ammonia nitrogen.
6. XANs: Autotrophic ammonia oxidizing bacteria (<i>Nitrosomonas</i> spp.)	6. SNO: Nitrate and nitrite nitrogen.
7. XANb: Autotrophic nitrite oxidizing bacteria (<i>Nitrobacter</i> spp.)	7. SSO4: Sulphate sulphur.
8. NH4N: Ammonium and ammonia nitrogen.	8. SH2S: Dithyrosulphide sulphur.
9. NO2N: Nitrite nitrogen.	Particulate components:
10. NO3N: Nitrate nitrogen.	9. XS: Slowly biodegradable particulate COD.
11. N2: Elemental nitrogen.	10. XI: Inert particulate COD.
12. PO4P: Phosphate phosphorus	11. XH: Heterotrophic bacteria.
	12. XA: Autotrophic nitrifying bacteria.
	13. XFB: Fermenting bacteria.
	14. XAMB: Acetotrophic methanogenic bacteria.
	15. XASRB: Acetotrophic sulphate reducing bacteria.
	16. XSQB: Sulphide oxidizing bacteria.
Organic nitrogen and organic phosphorus are modeled as part of the COD.	Organic nitrogen and organic phosphorus are modeled as part of the COD.
Nitrification is modeled as a two-step process. Bacteria are assumed to be immobile.	
It is generally assumed that all components except bacteria are soluble.	

Langergraber, G., and J. Šimůnek, The Multi-component Reactive Transport Module CW2D for Constructed Wetlands for the HYDRUS Software Package, Manual – Version 1.0, *HYDRUS Software Series 2*, Department of Environmental Sciences, University of California Riverside, Riverside, CA, 72 pp., 2006.
 Langergraber, G., D. Rousseau, J. Garcia, and J. Mean, CWM1 - A general model to describe biokinetic processes in subsurface flow constructed wetlands, *Water Science Technology*, 59(9), 1687-1697, 2009.

Wetland Modules: Processes

Processes: CW2D (Langergraber and Šimůnek, 2005) CWM1 (Langergraber et al., 2009b)

Heterotrophic bacteria:

1. Hydrolysis: conversion of CS into CR.
2. Aerobic growth of XH on CR (mineralization of organic matter).
3. Anoxic growth of XH on CR (denitrification on NO₂N).
4. Anoxic growth of XH on CR (denitrification on NO₃N).
5. Lysis of XH.

Autotrophic bacteria:

6. Aerobic growth of XANs on SNH (ammonium oxidation).
7. Lysis of XANs.
8. Aerobic growth of XANb on SNH (nitrite oxidation).
9. Lysis of XANb.

Heterotrophic bacteria:

1. Hydrolysis: conversion of XS into SF.
2. Aerobic growth of XH on SF (mineralization of organic matter).
3. Aerobic growth of XH on SA (mineralization of organic matter).
4. Anoxic growth of XH on SF (denitrification).
5. Anoxic growth of XH on SA (denitrification).
6. Lysis of XH.

Autotrophic bacteria:

7. Aerobic growth of XA on SNH (nitrification).
8. Lysis of XA.

Fermenting bacteria:

9. Growth of XFB (fermentation).
10. Lysis of XFB.

Acetotrophic methanogenic bacteria:

11. Growth of XAMB: Anaerobic growth of acetotrophic, methanogenic bacteria XAMB on acetate SA.
12. Lysis of XAMB.

Acetotrophic sulphate reducing bacteria:

13. Growth of XASRB: Anaerobic growth of acetotrophic, sulphate reducing bacteria.
14. Lysis of XASRB.

Sulphide oxidizing bacteria:

15. Aerobic growth of XSQB on SH2S: The opposite process to process 13, the oxidation of SH2S to SSO4.
16. Anoxic growth of XSQB on SH2S: Similar to process 15 but under anoxic conditions.
17. Lysis of XSQB.

Heterotrophic Organisms XH

Nitrosomonas XANs

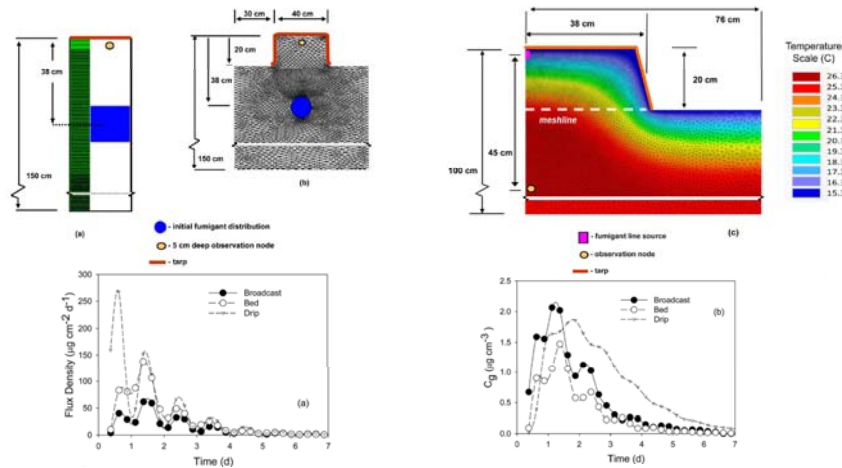
HYDRUS and its Modules

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- ◆ HYDRUS + Fumigant (fate and transport of fumigants)

HYDRUS + Fumigant

- ◆ HYDRUS-1D and HYDRUS (2D/3D)
 - Variably-Saturated Water Flow
 - Solute Transport
 - Heat Transport
 - Root Water Uptake
- ◆ Fumigant
 - Presence or absence of a Surface Tarp
 - Temperature dependence of Tarp properties
 - Removal of Tarp at specified time
 - Additional injection of fumigants into the transport domain at a specified location at specified time

Application of the Fumigant Module



Spurlock, F., J. Šimůnek, B. Johnson, and A. Tuli, Sensitivity analysis of vadose zone fumigant transport and volatilization, *Vadose Zone Journal*, 12(2), 12 pp., 2013.

HYDRUS and its Future Modules?

- ◆ **HYDRUS + Overland Flow** (surface runoff and overland flow)
- ◆ **HYDRUS + Freezing/Thawing, Meteo** (atmosphere)...
- ◆ **HYDRUS + Soil Mechanical Stresses** (effects of hydrological processes on slope stability)
- ◆ **HYDRUS + Global Optimization** (genetic algorithm, AMALGAM, DREAM, ...)
- ◆ **HYDRUS + MODFLOW** (hydrological processes at a large scale)

HYDRUS Web Site

Over 3 thousand downloads in 2008, over 5 thousand in 2009, and about 10 thousand downloads in 2010 and 2011; over 10 thousand registered members.

<http://www.pc-progress.com/en/Default.aspx>

HYDRUS Tutorials

Two-Dimensional Examples	Domain Design and FE-Mesh generation
	2.01 - 2D Domain composed of three irregular regions Video (1.2 MB) - Play - Download This demo demonstrates how to use multiple surfaces to define a single transport domain, and how these multiple surfaces can be used to assign various domain properties (e.g., materials).
	2.02 - 2D Domain with holes and integrated subregion Video (1.2 MB) - Play - Download This demo demonstrates how to design a complex two-dimensional transport domain that includes two holes and an internal surface. The transport domain is then discretized using a refined FE-Mesh inside of the internal surface.
	2.03 - 3D Domain, Solid 1 - three video tutorials Open tutorial This series of three demos shows how users can create a transport domain shown on the picture. The demonstration is divided into three parts. First, the main transport domain is defined, then a vertical hole is created in the domain, after which the heights are adjusted.
	2.04 - 3D Domain, Solid 2 - three video tutorials Open tutorial This series of three demos shows users how to create a transport domain shown on the picture and to discretize it into finite elements. We first create the transport domain, then add lines at the surface that will help us to discretize the transport domain into finite elements in the next step, after which we implement the finite element discretization.
	2.05 - 3D Domain, Solid 3 - three video tutorials Open tutorial This series of three demos shows users how to create a transport domain in the picture, to discretize the domain into finite elements, to create sections, and to specify initial and boundary conditions.
	2.06 - 3D Domain, Solid 4 - splitting a Solid into Sub-Layers and Columns Video (5.3 MB) - Play - Download This demo shows how to design a complex three-dimensional transport domain (which includes horizontal pipes). The transport domain is divided into four sub-layers (one with variable thickness). Additional FE-Mesh sections are generated as intersections of sub-layers and vertical columns. The use

HYDRUS Web Site: References

HYDRUS References

2009

- Li, H. Y., Zhu, T. H., Skaggs, and Z. Yu. Comparison of measured and simulated water storage in distant terraces of the Loess Plateau, China. *Agricultural Water Management*, 95(2), 299-306, 2009.
- McCoy, E. L., and K.R. McCoy. Simulation of putting-green soil water dynamics: Implications for turfgrass water use. *Agricultural Water Management*, 2008.

2008

- Akay, O., G. A. Fox, and J. Šimůnek. Numerical simulation of water flow during macropore/subsurface drain interaction using HYDRUS. *Vadose Zone Journal*, 7(3), 909-918, 2008.
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HYDRUS Projects - Drip

- Project Group:** Drip
- Description:** Examples involving subsurface drip irrigation; described in Hanson et al. (2006, 2008), Skaggs et al (2004), and Sijal et al. (2009).
- Availability:** Download HYDRUS projects now (11.1 MB)

Project	Description
Sub211a	Subsurface drip irrigation for the B fertigation strategy (fertigation near beginning of irrigation). Solutes considered: urea-ammonium-nitrate, potassium, phosphorus (Hanson et al., 2006).
Sub211c	Subsurface drip irrigation for the E fertigation strategy (fertigation near the end of irrigation). Solutes considered: urea-ammonium-nitrate, potassium, phosphorus (Hanson et al., 2006).
Sub213	Subsurface drip irrigation for the M50 fertigation strategy (fertigation during the middle 50% of the irrigation event). Solutes considered: urea-ammonium-nitrate, potassium, phosphorus (Hanson et al., 2006).
Sub1112	Subsurface drip irrigation, water table depth of 0.5 m, 0.3 dS/m, irrigation efficiency=0.9, 7 per week (Hanson et al., 2008).
Sub1212	Subsurface drip irrigation, water table depth of 0.5 m, 1.0 dS/m, irrigation efficiency=0.9, 7 per week (Hanson et al., 2008).
Sub2111	Subsurface drip irrigation, water table depth of 1.0 m, 0.3 dS/m, irrigation efficiency=0.9, 2 per week (Hanson et al., 2008).

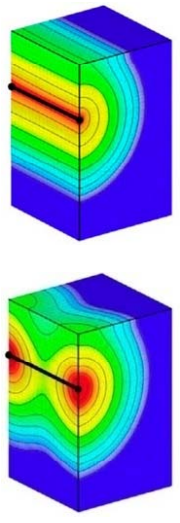
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Mathematical/Numerical Models

Mathematical Models have the potential to be powerful tools to help understand and quantify the complexities of various processes in the subsurface.

Mathematical Models are:

- ♦ a repository for currently available knowledge
- ♦ represent a practical tool to improve our understanding of and ability to quantify various processes

Meaningful applications of **Mathematical Models** include:

- ♦ predicting outcomes under given assumptions
- ♦ testing hypotheses
- ♦ identifying conditions and locations of increased risk
- ♦ developing treatment strategies, and
- ♦ informing management decisions

However, it should be acknowledged that **Mathematical Models** are not expected to be precise predictors of reality, but are only as good as their input parameters and modeling assumptions.

Questions and Suggestions?

Thank you for your attention

